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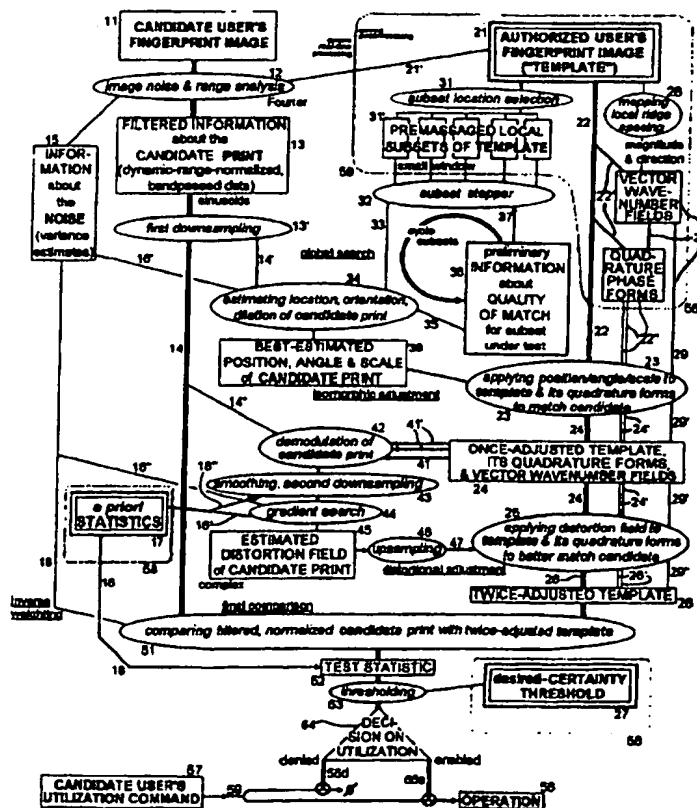
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(54) Title: SYSTEMS AND METHODS WITH IDENTITY VERIFICATION BY COMPARISON AND INTERPRETATION OF SKIN PATTERNS SUCH AS FINGERPRINTS

(57) Abstract

A sensor receives a print image from an authorized person (21) to form a template, and from a candidate (11) to form test data. Noise variance (12) is estimated from the test data as a function of position in the image, and used to weight the importance of comparison with the template at each position. Test data are multilevel, and are bandpassed and normalized (13) and expressed as local sinusoids for comparison. A ridge spacing and direction map (28) of the template is stored as vector wavenumber fields, which are later used to refine comparison. Global dilation (34) and also differential distortions (45) of the test image are estimated, and taken into account in the comparison. Comparison yields a test statistic (52) that is the ratio, or log of the ratio, of the likelihoods of obtaining the test image assuming that it respectively was, and was not, formed by an authorized user. The test statistic is compared with a threshold value, preselected for a desired level of certainty, to make the verification decision.



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SYSTEMS & METHODS WITH IDENTITY VERIFICATION BY COMPARISON
& INTERPRETATION OF SKIN PATTERNS SUCH AS FINGERPRINTS

5 RELATED PATENT APPLICATIONS

Two coowned patent documents of Areté Associates, Inc., are wholly incorporated by reference herein: PCT/US96/01615, based on a U. S. application of Bowker and Lubard; and copending attorney docket
10 xAA-38, filed in the PCT concurrently herewith on September 8, 1997, based on a U. S. application of Bowker et al., and entitled "ECONOMI-
CAL SKIN-PATTERN-ACQUISITION APPARATUS FOR ACCESS CONTROL; SYSTEMS CONTROLLED THEREBY", later made PCT/US97/_____.

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FIELD OF THE INVENTION

This invention relates generally to systems and methods for verifying identity of people, by comparison and interpretation of skin
20 patterns such as fingerprints; and more particularly to novel firmware and software stored in apparatus memories, as portions of apparatus, for interpreting such patterns and controlling utilization devices. With respect to certain of the appended claims, the invention further relates to systems that include such utilization devices.

25 A utilization device is, for example, a facility, apparatus, means for providing a financial service, or means for providing information. The phrase "utilization device" thus encompasses, but is not limited to, businesses, homes, vehicles, automatic teller machines, time-and-attendance systems, database-searching services, and
30 a great many other practical systems. An apparatus memory for such storage is, for example, a programmable read-only memory ("PROM"), or a computer-readable disc.

35 BACKGROUND OF THE INVENTION

Classical methods for evaluation of fingerprints. toeprints, palmprints and like skin patterns entail location, categorization and tabulation of minutiae are fundamentally limited by their sensitivity
40 to measurement noise at the location of the minutiae. Automated analysis based on minutiae also is inherently very dependent on image

enhancement — which often breaks down when initial data quality is marginal.

A few relatively sophisticated patents use digital computers to (1) automatically select one or more distinctive small regions — not necessarily minutiae — in a master print or "template", and then (2) automatically look for one or more of these selected small regions in a print provided by a person who purports to be the maker of the template. These earlier patents particularly include U. S. 5,067,162 of Driscoll, 5,040,223 of Kamiya, 4,982,439 of Castelaz, 4,805,223 of Denyer, and 4,803,734 of Onishi.

All of these latter patents describe making final verification decisions based upon such comparisons of small regions. They depend excessively upon isolated, small amounts of data — very small fractions of the available information in a candidate user's print.

Some of the patents in the above list do describe sound techniques for one or another part of their respective processes. Some workers, such as Driscoll and Kamiya, use electronic correlation methods to choose the small reference sections in the enrollment process — i. e., in forming the template — and also in comparison of those regions with features in a candidate user's print. Denyer similarly uses an approximation to such correlation technique.

These patents do generally allow for the possibility that the authorized user's template may be shifted, or in other words translated, in placement of the print image on the sensor. Some (particularly Driscoll and Denyer) allow for the possibility that the template may be rotated too.

Driscoll discusses finding a least-squares-fit between plural reference regions and a potentially corresponding plurality of test regions in the candidate print. He suggests that departures from an ideal rotated pattern of the reference regions is to be accounted for by distortion of the fingertip in the course of placement on a sensor, but by his least-squares approach also suggests that such distortion is inherently "random" in the sense of lacking internal correlation.

Whereas distortions of flesh-and-skin structures are in fact random in the sense of being modeled or modelable statistically, proper efforts at such modeling must take into account that neighboring portions of the structure exert influences upon one another, resulting in physical correlations. In short, neighbors are softly constrained.

Driscoll's approach, in using a least-squares fit — to accommodate departures from a rigid rotation that underlies the distortion — in essence disregards such correlations; at best, he only considers a

small part of the operative statistics. Denyer, too, briefly mentions (though in a much more generalized and tangential way) the possibility of somehow accounting for distortion.

All of these patents, however, fail to take account of dilations
5 (or, to put it more completely, dilations or contractions) which an authorized user's fingertip may undergo — relative to the same user's established template. Such dilations may arise from variations in the pressure with which the finger is applied to an optical or other sensor (capacitive, variable-resistance etc.).

10 Such dilations may be expected to have at least a component which is invariant across the entire image, in other words a dilation without change of fingerprint shape — an isomorphic dilation. Furthermore all the above-mentioned patents fail to make systematic, controlled allowance for dilations and other forms of distortion that are
15 differential — which is to say, nonisomorphic.

Correlation methods, matched-filter methods, and (loosely speaking) related overlay-style techniques of comparison all fail totally in any area where a reference print is mismatched to a candidate print by as little as a quarter of the spacing between ridges. I have found
20 that dilations and other distortions can and commonly do produce spurious mismatches locally — over sizable areas — exceeding twice the spacing between ridges, that is, many times the minimum disruption which destroys correlation and thereby recognition.

Therefore, failure to account properly for either dilation (iso-
25 morphic distortion) or distortion (differential distortion) results in unacceptably high rates of failure to verify or recognize an authorized user — i. e., high rates of the so-called "false rejection" or "type 1 error". Artificial measures aimed at reducing this failure rate lead inevitably to the converse: unacceptably high rates of
30 failure to reject unauthorized users, impostors — i. e., high rates of the so-called "false acceptance" or "type 2 error".

Merely allowing for some distortion, in a statistically uncontrolled way, can never cure this fundamental failing. Skin and flesh distortion does not affect prints in an uncorrelated way, but rather
35 in partially systematic ways that arise from the physical character of skin and flesh. I believe that failure to account properly for distortion is the single greatest contributor to poor performance of fingerprint verifying systems heretofore.

Furthermore variations in habits of placement of a fingertip on a
40 sensor tend to be somewhat systematic. These systematic properties of

the print-forming process have their own statistically characteristic patterns — their own statistics.

In the context of any given comparison method, these special statistics exert particular characteristic effects on the results.

5 All the patents mentioned above appear to ignore these statistics, in the process discarding very important information that bears strongly on verification decisions.

In addition, the patents listed above fail to make use of modern principles of decision theory and signal processing that have been
10 used to great advantage in other fields. Driscoll, for instance, while discussing the final stages of his analysis in terms reminiscent of the established Neyman-Pierson analysis, does not appear to properly apply the principles of that analysis. Such principles have been importantly applied in industrial, military, and scientific pattern-
15 recognition problems, but workers in the practical fingerprint field do not appear to be aware of these principles or in any event are not evidently using them.

Similarly none of the patents noted makes use of decisional down-weighting of data from areas that are less certain or noisier; rather,
20 to the extent that any consideration at all is given to such matters, noisy data are simply discarded — a very undesirable way to treat expensive data. Bandpassing of test data is not seen in these references, although certain other forms of filtering are used by Driscoll and others. Normalizing is likewise absent — except for trivial
25 forms implicit in binarization or trinarization, used in many print analyzers. None of the noted patents teaches expression of test and template data, or comparison of such data with one another, in terms of local sinusoids.

30 Thus the skin-pattern verification field has failed to make good use of all available data, take effective account of dilations or distortions, make suitable allowance for known statistics of placement variation, and apply modern decisional and signal-processing tools. As can now be seen, the prior art in this field remains subject to
36 significant problems, and the efforts outlined above — although praiseworthy — have left room for considerable improvement.

SUMMARY OF THE DISCLOSURE

The present invention introduces such improvement, and performs
40 fingerprint verifications with an outstandingly high accuracy not

available heretofore. The invention has several facets or aspects which are usable independently — although for greatest enjoyment of their benefits I prefer to use them together, and although they do have several elements in common. The common parts will be described
5 first.

In its preferred apparatus embodiments, the present invention is apparatus for verifying the identity of a person. It operates by comparing (1) test data representing a two-dimensional test image of that person's skin-pattern print with (2) reference data derived from a
10 two-dimensional reference skin-pattern print image obtained during a prior enrollment procedure. Each of the apparatus embodiments includes some means for holding instructions for automatic operation of the other elements of the apparatus; these instruction-holding means include or make use of a nonvolatile memory device, and may be termed
15 the "nonvolatile memory means".

Now in preferred embodiments of a first of its independent aspects, the apparatus includes some means for extracting from the test data an estimate of noise variance in the test data. For purposes of breadth and generality in expression of the invention, these
20 means will be called simply the "extracting means"; they extract a noise-variance estimate as a function of position in the test image.

The apparatus of this first facet of the invention also includes some means for comparing portions of the test and reference data, for
25 corresponding positions in the two images. Once again for generality and breadth these means will be called the "comparing means".

In addition the apparatus includes some means for weighting the importance of comparison for each portion. These means — again the "weighting means" — weight the importance of comparison for each
30 portion in accordance with the noise-variance estimate for the corresponding position.

Also included are some means, responsive to the weighting means, for making an identity-verification decision — identified here as the "decision-making means".

35 The foregoing may be a description or definition of the first facet or aspect of the present invention in its broadest or most general terms. Even in such general or broad form, however, as can now be seen the first aspect of the invention significantly contributes to resolving the previously outlined problems of the prior art.
40 In particular, the use of downweighting for noisier regions of a print is a major step toward enabling use of essentially all available data.

Now turning to a second of the independent facets or aspects of the invention: in preferred embodiments of this second facet, the invention apparatus includes some means for deriving from the test data corresponding multilevel test data that are bandpassed and normalized.
5 For reasons suggested earlier these means may be denoted the "deriving means".

For the purposes of this document the term "normalize" is to be understood as describing a true stretching (or compression) of the dynamic range of data to a standard range — while maintaining multi-
10 level character of the data. This normalization thus is understood to be beyond the trivial forms seen in prior-art binarization and trinization, which force all data to be only binary or at most trinary.

This apparatus also has comparing means related to those described above for the first aspect — but here the comparing means are
15 for comparing portions of the bandpassed and normalized multilevel test data with the reference data. In addition it has decision-making means, also related to those described earlier — but here the decision-making means are responsive to the comparing means.

The foregoing may constitute a definition or description of the
20 second facet or aspect of the present invention in its broadest or most general terms. Even in such general or broad form, however, as can now be seen the second aspect of the invention resolves the previously outlined problems of the prior art.

In particular such an apparatus by taking advantage of signal-
25 enhancing techniques of bandpassing and normalization improves both actual signal-to-noise relations and effective signal-to-noise relations in the system, in terms of best use of the available data-handling capability.

These advantages have not heretofore been enjoyed by skin-pattern
30 verification systems. In this way this second facet of the invention too leads toward greater precision and accuracy in verifying prints.

In a third of its independent facets, the invention apparatus includes means for expressing the test data in the form of local
35 sinusoids, and means for expressing the reference data in the form of local sinusoids. The apparatus also includes comparing means — but here the comparing means compare portions of the sinusoidally expressed test data with the sinusoidally expressed reference data.

Decision-making means are also included, responsive to the com-
40 paring means as just defined. By operating on the data in sinusoidal form the invention in preferred embodiments of this third aspect is

able to exploit many advanced signal-processing techniques, particularly including the Fast Fourier Transform (FFT), multiplicative operations in the frequency domain in lieu of convolutions in the spatial domain, back-transformations to find spatial results etc. — each of
5 which saves a great amount of computational time and effort without loss of accuracy. Neither sinusoidal representations nor Fourier treatment of digital data has heretofore been used in this field.

Preferred apparatus embodiments of the invention in a fourth of
10 its independent facets include some means for deriving from the reference data a map of ridge spacing and direction. These deriving means also store the map as one or more vector wavenumber fields.

Further included are some means for comparing portions of the test data with the reference data; these comparing means include means
15 for using the vector wavenumber fields to refine the comparing operation. The apparatus also includes decision-making means responsive to these comparing means.

While some earlier systems do make one or another type of ridge map, typical earlier uses proceed to direct comparison of the maps.
20 None stores the map in the form of a vector wavenumber field for later use in refining a discrete comparing operation.

This aspect of the invention enables several extremely effective uses of the ridge spacing and direction data in adjustments of the authorized-user template for fairer comparison with a candidate user's
25 fingerprint. Such advantages will be more clearly seen in later sections of this document.

Apparatus of preferred embodiments according to a fifth independent aspect or facet of the invention includes some means for estimating
30 the assumed dilation of the test image relative to a reference image — i. e., "dilation-estimating means". The dilation here mentioned is to be understood as having a global character — in other words, affecting the entire print uniformly, without change of shape. The dilation-estimating means thus estimate isomorphic dilation.

35 The apparatus also includes means for comparing the test data with the reference data, taking into account the estimated dilation. The apparatus also includes decision-making means that respond to these comparing means.

This facet of the invention too advances the art meaningfully as
40 it enables two major operating improvements. The first of these is finding small regions of a candidate-user print that correspond to

selected distinctive regions of the authorized-user template — even in the presence of dilations that would otherwise destroy the correlation and so impair recognition.

The second major operating improvement attributable to this fifth independent aspect of the invention is particularly efficient operation of a more-general distortion-estimating aspect of the invention that will be described below. My global-dilation evaluating feature gives the later distortion estimator a running start, in that the distortion estimator need seek only the spatially differential part of the overall distortion — perturbations, in other words, of the global, isomorphic dilation.

Apparatus according to a sixth independent aspect of the invention includes some means for estimating an assumed distortion of the test image relative to a reference image. Here the distortion under discussion particularly includes nonisomorphic distortion.

As will be understood, however, the distortion here mentioned typically also includes an isomorphic component — to the extent that previous detection of and accounting for isomorphic dilation was imperfect, or perhaps was not provided at all. The apparatus also includes means for comparing the test data with the reference data, taking into account the estimated distortion; and decision-making means responsive to these comparing means.

Although all the independent aspects and facets of my invention make extremely important contributions to excellent performance of my invention, the distortion-estimating means resolve the root cause of what I consider the greatest single defect in prior systems. As suggested earlier, it is this defect that especially impairs the ability of prior systems to reliably recognize an authorized user — i. e., to recognize a clear, clean template which has simply been slightly distorted.

In particular the estimation of distortion enables application of the estimated distortion to approximately equalize test and reference data with respect to the assumed distortion. The comparing means can then compare the thus-approximately-equalized test and reference data.

This can be done particularly straightforwardly, by using the estimated distortion to generate a matched filter for use in forming a test statistic. In both the filter generation and the actual use of the test statistic thereby formed, the system can readily be made to take into account estimated noise variance in the test data, as a function of position in the test image.

The distortion adjustment underlies and enables all such refinements. The result is an overall level of excellence in recognition of templates, even in the presence of unusual distortions — leading in turn to truly extraordinary low error rates of both the "false rejection" and "false acceptance" types.

Operating details of the distortion-estimating means — including demodulation of the test data, smoothing, downsampling and then a cautiously expanding gradient search for the assumed distortion field, to avoid loss of phase registration — will all be presented below.

10

In a seventh of its independent facets or aspects, preferred apparatus embodiments of the invention include some means for comparing the test data with the reference data to form a test statistic as the ratio, or logarithm of the ratio, of the likelihoods of two contrary hypotheses:

likelihood of obtaining the test image, assuming that the candidate user is the same person who also formed the reference fingerprint image (template), and

20

likelihood of obtaining the test image, assuming that a different person formed the reference print image.

This apparatus also includes decision-making means responsive to the test statistic.

This aspect of the invention thus for the first time in the fingerprint field makes proper use of established principles of decision theory. Print verifications are thereby placed on a sound footing that actually leads to the most conclusive decision that can justifiably be made from the available information — no more, no less.

Fingerprint-based identity verifications have long suffered from absence of such sound basis. Advantageously my comparison means are combined with means for comparing the test statistic with a threshold value preselected to impose a desired certainty level in verification.

35

In yet another independent facet or aspect of my invention, preferred embodiments of the invention take the form of a method, rather than apparatus. This method is for verifying the identity of a person. The method does so by comparing test data representing a two-dimensional test image of that person's skin-pattern print with refer-

40

ence data derived from a two-dimensional reference skin-pattern print image obtained during a prior enrollment procedure.

The method includes the step of extracting from the test data an estimate of noise variance in the test data as a function of position 5 in the test image. It also includes the step of comparing portions of the test and reference data, for corresponding positions in the two images.

Furthermore the method includes the steps of weighting the importance of comparison for each portion, in accordance with the noise- 10 variance estimate for the corresponding position; and — responsive to the weighting means — making an identity-verification decision. Another step is, in nonvolatile memory, holding instructions for automatic operation of the foregoing steps. Thus the method partakes of the advantageousness of the noise-weighting apparatus embodiments 15 of the first independent aspect of the invention, discussed earlier.

All of the foregoing operational principles and advantages of the present invention will be more fully appreciated upon consideration of the following detailed description, with reference to the appended 20 drawings, of which:

BRIEF DESCRIPTION OF THE DRAWINGS

Fig. 1 is a flow chart or block diagram showing, for certain preferred embodiments of my invention, how different portions of the 25 programmed firmware perform the processes of the invention;

Fig. 2 is a rough conceptual presentation of a windowed subset of the authorized-user template, arrayed with sixty-three isomorphs of that subset — nine rotations and seven dilations (including the original);

30 Fig. 3 is a rough conceptual diagram of the original subset of Fig. 2 in position in the authorized-user template, and one of the nine-by-seven array of isomorphs linking that template with the candidate data;

Fig. 4 is a rough conceptual diagram, conveying the general 35 principle of applying a distortion field to modify the template;

Fig. 5 is a highly enlarged conceptual diagram of a whorl area in a fingerprint, particularly illustrating changes of interridge phase in the area;

Fig. 6 is a graph or diagram showing relationships of a very 40 general representative "test statistic";

Fig. 7 is a like view for a test statistic 52 of Fig. 1, in accordance with the present invention; and

Fig. 8 is an overall block diagram showing the embodiment of my invention in a hardware system.

5

DETAILED DESCRIPTION
OF THE PREFERRED EMBODIMENTS

Inputs — As Fig. 1 shows, preferred embodiments have at least three groups of inputs: one group of inputs from the candidate user of a weapon or other apparatus, another from the authorized user (or that person's surrogates), and the third from generalized population data. The candidate's inputs include a fingerprint-image data array 11 and a command 57 (at bottom left in the drawing) that the apparatus operate. The data array 11 originates from a skin-pattern detector, which is most representatively an optical sensor array but may instead be of another type such as capacitive, variable-resistive or high-frequency acoustic.

The authorized user's inputs include a fingerprint-image data array 21 (originating analogously to the array 11 for the candidate user, discussed above), and a parameter setting 27 which reflects the desired certainty with which a fingerprint match must be found. The authorized user does not necessarily personally enter this parameter 27 into the system, but may instead indicate a selection of the value, or acquiesce in the value, of this parameter.

The desired-certainty threshold parameter 27 is related to the relative numbers of false positives and false negatives to be tolerated — but not in an arithmetically direct way, rather in complicated statistical ways as will be explained in further detail later in this document. For this reason, a more precisely correct name for this threshold parameter 27 might be more abstract, e.g. "decision threshold"; however, the phrase "desired-certainty threshold" may be more helpful as it is more descriptive.

This value is selected to reflect the type of usage anticipated. In particular, it can be related to the probability of false negatives, so that it could be thought of as controlling the "desired certainty" of acceptance for the authorized user. Alternatively, the desired-certainty threshold can be inversely related to the probability of false positives, and thought of as controlling (but in an inverse way) the desired certainty of rejection for an unauthorized user.

For example, if the apparatus is to control access to an advance-fee-based gymnasium, the primary objective may be merely to discourage occasional cheaters. In this case the certainty of acceptance for the prepaid customer or member of the gym may be set very high — accepting a significant chance of letting in someone who has not paid.

Similarly if the apparatus is a weapon to be used in the field by military or police personnel, a primary objective may be to have use of the weapon available to the authorized user without delay and without question. In this case the certainty level may be set relatively high — accepting some small chance that the weapon might be usable by an opponent who takes it from the authorized user. In this case, however, since there are significant risks associated with an opponent's appropriation of a weapon, the authorized-user acceptance likelihood might not be set quite as high as in the first example above where the adverse consequences of admitting a cheater are minor.

Now in a contrary example, for control of access to a secure area containing documents or apparatus of utmost sensitivity, a primary objective may be to exclude spies. In this case, certainty level for acceptance of authorized personnel may be set distinctly low — accepting some significant likelihood that an authorized individual may be delayed in entry by having to repeat the verification procedure.

Similarly if the apparatus is a weapon to be kept in a home for protection against intruders, a primary objective may be to prevent unauthorized use by children or teenagers who live or visit in the home. In this case the certainty level may be set relatively low — accepting some small degree of unreliability in the weapon's availability for use against intruders — but perhaps not as low as in the immediately preceding example, since delayed availability of a weapon to an authorized user in an emergency is ordinarily much more onerous than delayed entry to a secure area.

A third type of input is a statistical set 17 preferably coming from neither the candidate user nor the authorized user, but rather from a generalized database representing people in general. Since these data are ordinarily derived without reference to the particular people known to be involved, I call these data "prior statistics" or "a priori statistics".

The statistical data 17 are applied 18, 18" at certain points in the processing to take into account the known degree of variability in the way people place their fingers on a fingerprint-acquisition

imaging device. This variability may differ depending on the position and orientation of the imaging device in relation to the user.

For example, variability in a panel-mounted imager at an automatic teller machine may be expected to have a statistical pattern that is different from variability in a desktop imager in an office. Variability in an imager that is built into a tool (e. g., a weapon) may be expected to be different still.

In some cases, particularly where a user typically is standing while applying a fingertip to a stationarily mounted imaging device, this variability may vary with height of the user. In any event it is preferable to collect a different a priori data set using the actual imager type and collection geometry for which a particular apparatus will be used. In extraordinary cases, initial data acquisition may show that the authorized user's prints have very unusual properties or characteristics; and better performance may result from using a statistical set 17 derived from input data 21 for the authorized user.

Procedural overview — A glance at the bold vertical lines 14, 22 in Fig. 1 reveals the fundamental scheme, to direct signals 12-14 from the candidate fingerprint image data 11, and signals 22-26 representing the authorized user's preprocessed fingerprint image data or "template" 21, to a common final comparison 51. Side calculations or signal paths 15-16, 28-47 along the way facilitate or enhance the result.

Results 52-56 of the comparison 51 interact with signals 59 generated by the candidate's command 57 — in a manner controlled by the desired-certainty threshold 27 — to determine whether the command 57 produces no perceptible action at all ϕ , or operation 56. (The invention encompasses including a no-function warning light or tone, rather no perceptible action, if use is denied 55d.)

30

Preliminary processing of the candidate's data — Processing of the candidate image data 11 begins with analysis 12 of the dynamic range of signals which represent grooves and ridges within the image. The result includes forming a new image-data version 13, in which this dynamic range is normalized, i. e. locally stretched or compressed to precisely match the overall range of the later processing stages.

In addition the new version of the image is subjected to Fourier analysis — expressing the data as spatial sinusoids — and bandpass filtering, to eliminate inappropriate spatial frequencies in the image version 13. In the analysis 12, preferably spatial frequencies are treated as "inappropriate" if they are not spatial frequencies 21'

that could have originated from the similarly preprocessed print (template) 21 of the authorized user.

Preprocessing of the authorized user's print to obtain the template will be described shortly. In such original preprocessing, spatial frequencies can be rejected based on a more leisurely harmonic-content analysis of the user's print.

Closely associated with the range analysis 12 and resulting bandpassed, normalized sinusoidal data 13 is a downsampling step 13' which greatly reduces the amount of data to be processed in all later stages of the procedure. This step 13' is important: it can make the difference between a procedure that is unacceptably time consuming and one that is practical.

Of course it is also important that the procedure be accurate. Properly controlled downsampling at this step, however, does not degrade overall performance. It is known that the data 13 are represented sinusoidally, and that these data cannot have major components at finer spatial frequencies than the smallest spacing of troughs or ridges in the authorized user's print 21. Accordingly, in downsampling 13' it suffices to preserve representative values at a reasonable fraction less than half of that smallest periodicity — or for example about one third of the average periodicity. Once again the template frequency content 21' is useful, in guiding selection of an optimum spatial frequency for use in the downsampling step 13'.

Philosophical overview — Four important characteristics of the invention can be gleaned already from the foregoing discussion of blocks 12 through 13' in Fig. 1. First, the assumption is made throughout that the candidate user is the authorized user — and that this assumption can be confirmed, if only we conduct a fair comparison.

It might be supposed that this assumption will lead to an overwhelming number of false-positive test results. Such a supposition would be incorrect, for I have found that a fair comparison will only highlight the underlying differences in information content between an unauthorized candidate (impostor) and the true authorized user.

The present detailed description, as it unfolds, will make progressively more apparent that each intermediate process step 23-47 of my invention — when practiced upon a typical impostor's print — is most likely to lead to catastrophic misalignment of the two prints.

By far the most likely end result, in the final decision 54, is a decisive denial 55d.

The assumption under discussion is also confirmed from the opposite perspective: what happens if the candidate user is in fact the authorized user? A fair comparison is absolutely essential to eliminating the effects of enormous variation in fingerprint appearance due to details of operating conditions. Such details include, in particular, the physical and emotional condition of the user — and these considerations are especially important to avoid rejecting the authorized user.

Thus the assumption that the candidate is the authorized user only leads to very great reduction in amount of data to be processed, and very great increase in reliability of results.

A second characteristic of the invention is an overriding plan to form respective versions of the two data sets 11 and 21 which are adjusted to be as much alike as possible. This adjustment, however, is only with respect to certain data properties that are known to be variable within multiple trials or instances of essentially any single user to form a print.

These particular variable data properties, within their known degree of variability, are at best immaterial (and at worst misleading) to identification or verification. The invention is accordingly fashioned to ferret them out, so that they can be canceled out — in a word, to ignore them.

In doing so, it is necessary to accommodate the extreme time pressure associated with the candidate-data processing. Conversely, relatively long times can be devoted to obtaining several instances of an authorized user's print — and selecting the most representative one(s) of them, and performing image enhancement thereon. It is desirable to take advantage of the available time to perform such extra steps, though it only very occasionally turns out to have been necessary.

The shaded lines 58 enclose those portions of the data collection and processing that can be performed in advance, before deploying the apparatus or receiving the candidate user's command. These portions include establishment of a statistical set 17 and the desired-certainty threshold 27, as well as the authorized-user data collection and processing 21 through 22", and 28 through 31'.

A third characteristic of the invention is closely related to the first two. This characteristic is that the invention makes the template as clean and as definite as possible — and then exploits that fact by primarily relying upon the template, rather than upon the candidate data, wherever feasible.

A first example of this is in the preferred use of the template to provide periodicity criteria 21' for both the analysis 12 and downsampling 13' — rather than relying upon statistics of the candidate data 11 for the bandpassing criteria. This strategy is preferred even though the analysis 12 does in fact extract those candidate-data statistics 15 for other purposes.

Later examples of this characteristic of the invention will be seen shortly in the preprocessing selection 31 and premassaging of numerous local subsets 31' of the template 21. This characteristic will be seen also in the preprocessing preparation 28 of local ridge-spacing maps and vector wavenumber fields 29; and also highly specialized gradient 22' and quadrature forms 22" derived from the template 21 and wavenumber fields 29.

A fourth characteristic of the invention is that it operates on the data in terms of local sine-wave patterns, rather than as isolated binary data bits or linear (ridge and groove) structures. Thus the initial noise and range analysis 12 operates not only in positional space but also in Fourier space (in other words, in terms of the spatial frequencies in the candidate image), and the new version or filtered information 13 is presented as amplitudes of sinusoids associated with each region of the original image.

By virtue of this characteristic, while guided by detection theory the invention can also take advantage of the high computational efficiency and fidelity of the Fast Fourier Transform (FFT). The FFT performs a large fraction of the computationally intensive processes in the algorithm.

Preprocessing of an authorized user's print images — During preprocessing 58 the authorized user provides a fingerprint that will be refined to form a template 21. Details of the refinement will be discussed shortly.

Where time permits, best results are obtained by acquiring several realizations, or successive trial images, of the authorized user's print — and analyzing them to determine which is most representative and whether they have any extraordinary character that may require

special handling. From the representative authorized-user print image or images 21, in preprocessing 58 the system selects 31 several distinctive regions, subsets or windows 31'. These small, preferably circular regions 31' are stored separately from the full template 21 — as are (preferably for certain embodiments) numerous versions or variants of each region, prepared by applying a variety of crosscombinations of various-sized rotations and dilations.

Since this part of the procedure is performed during preprocessing 58 rather than later during decision-making time, there is great freedom to calculate the rotations and dilations by any of various procedures — such as, e.g., by oversampling and interpolation. For reasons that will appear shortly, however, the regions/variants 31' are preferably stored as Fourier transforms, rather than directly as spatial data.

Nevertheless it is preferable to calculate these transforms expeditiously. Preferably the procedure known as a "Fast Fourier Transform" (FFT) is used, although this precludes a single-step transformation in two dimensions. Two one-dimensional FFTs can be calculated more quickly.

Other important data 21', 29, 22', 22" are also advantageously extracted from the template 21 during preprocessing, making best use of the more leisurely time available for this work. Already mentioned are the statistics 21' for use in the image noise and range analysis 12 of the candidate image 11.

This information is found through data conditioning akin to that 12 which is discussed elsewhere in this document in relation to candidate data. Also found through such data conditioning are normalized, bandpassed data, and vector gradient fields 22' (somewhat closely related to the template data 22).

In addition, a so-called "matrix covariance estimator" is used to map 28 magnitude and direction of local ridge spacings in the template 21 — to form vector wavenumber fields 29, which will be used later in forming the final template 26 for comparison 51 with the candidate data 14. During preprocessing 58 these fields 29 also are combined (not shown) with the input template data 21 in such a way as to provide smoothing along ridge lines, in the output template data 22; and moreover are also multiplied by the template gradient 22' to form two quadrature-phase forms 22" of the template data 22.

These quadrature forms 22" too will be used in forming the final template 26 for comparison — and also particularly in beginning 42 to isolate differential distortion 45 in the candidate print. During

real-time processing, as shown, the two quadrature forms 22" and the wavenumber fields 29 will all be modified twice 23, 25 — keeping them in step 24', 29', 26', 29" with the modified direct template data 24.

In addition, flags are set up in certain of the vector wavenumber fields 29 to warn of phase reversals in the template data 22, as will be explained below. These warning flags are used in selecting one or the other of the quadrature phase forms 22", 24', 26' of the template for use. This enables the system to avoid errors that would otherwise arise in allowing the processing to continuously traverse phase discontinuities.

Further specifics of these preprocessing steps will be introduced below in discussion of the processing stages that make use of these special preprocessed data.

15 Using candidate-data variance estimates — The above-discussed initial noise analysis 12 in the candidate-data (left) half of Fig. 1 may be considered roughly as a data colander, which separates data from noise. Both the data and the noise are then suitably directed, respectively, for beneficial use.

20 Fig. 1 shows that the data and the noise actually proceed to many of the same later stages of the algorithm, in the sense that the later processing blocks 34, 44, 51 receive both data and noise. In each of the later processing modules, however, these different pieces of information are separately received and very differently used.

25 Thus one of the above-mentioned side-calculation paths is application of the noise information 15 abstracted from the candidate data to enhance later stages of processing. This information 15 is in the form of an array or field of variance estimates, in effect overlaid on the reformed image data 13.

30 In other words the system constructs and keeps a separate index 15 of the reliability of the image data 13 in each region of the image, respectively. These reliability indices are used to weight the respective significance that is attributed to each comparison or other calculation based upon data in the corresponding image regions.

35 Thus for instance the noise variance array 15 is applied 16 to the final comparison step 51, so that the final test statistic (measure of probable identity between candidate and authorized user) 52 depends more heavily on portions of candidate data 11 that are relatively cleaner. The test thus depends more lightly on portions that
40 are relatively noisier.

Such use of downweighted information, where the information is of lesser reliability, is far superior — in making maximum use of available information — to merely setting an arbitrary criterion of reliability and then discarding questionable information. The latter
5 technique appears, for example, in Driscoll's selection of a very small number of "best-match" regions, and then proceeding directly to final decision based on such regions.

For any given intensity of calculation, and any given noisiness and distribution of noisiness in the candidate data, the downweighting
10 maximizes the reliability of the results at each point in the procedure — and overall. For like reasons the noise array 15 is also applied 16', 16" to control certain others of the previously mentioned side calculations.

15 Global search & isomorphic adjustment: purpose — Another side calculation 31-38 yields a measure of simple (shape-invariant) geometrical mismatches in the formation, or realization, of the candidate print image 11, relative to the template 21. By the terms "formation" and "realization" I mean to distinguish variations in placement of a
20 fingerprint from the information content of the candidate print itself.

Preferably for certain embodiments this second side calculation 31-38, like the first, is partially performed in preprocessing time 58. This side calculation 31-38 accounts for displacements or trans-
25 lations of the entire image, rotations of the entire image, and also dilations or contractions of the entire image resulting from variation in pressure with which the entire fingertip is pressed against the sensor. As will be understood, when increased pressure squashes the whole surface of the fingertip against the receiving surface, the
30 whole fingertip surface may expand slightly — but preserving the original shape, i. e. isomorphically.

Of course the authorized user's initial print is taken with some applied pressure, so each candidate-print realization may be made with either more or less pressure than applied in making that initial
35 print. Hence the size change if characterized as "dilation" may be either positive or negative — or, if multiplicative, as a factor greater or less than unity.

The global search is "global" in two senses: first, the entire candidate print is canvassed to find one or more regions that most
40 closely match preidentified portions of the template. Second, once the one or more best-match regions are found the remaining mismatch is

treated as a positional/dilational error with respect to the entire useful area of both prints.

Identifying comparison regions for global search — Comparison regions 31, also called "local subsets" of the template 21, are first identified 31 (and if desired their data separately stored) during preprocessing 58. They are identified 31 as regions that have some particularly distinctive character.

Such distinctiveness may be defined for example in terms of high rates of change of harmonic content. If preferred, within the scope of my invention they may instead be defined in more conventional ways — such as closely adjacent plural/multiple ridge or groove endings.

In the preferred embodiment, the choice of subset is made by locating a circular subset window in such a way as to minimize the values of the crosscorrelation function of the windowed subset versus the entire template image — at nonvanishing offset values. Preferably plural windows are established 31 in this way, each under the assumption that any already-established windowed region is unavailable.

In any event it is important that the selected windows contain essentially the most distinctive features of the authorized user's print, since they will be used to guide the process of adjusting the template to match the candidate. If the features used were instead relatively common, the system would be more likely to perform the adjustment incorrectly even if the candidate is the authorized user — resulting in a false-negative finding 55d.

Each of the local subsets selected 31 represents a view of a small part of the template, as seen through a small window. The size of the window is important: it must be large enough to contain a moderately complex and therefore truly distinctive set of features; but small enough to preserve correlation — i. e., enable recognition — of its distinctive features when allowance is made for isomorphic translations, rotations and dilations, and even if the fingerprint has undergone more general locally-varying distortions. Also preferably the several identified 31 subsets are reasonably well separated from each other, or they may not be independent enough to complement each other in the ways to be described.

In later real-time comparison processing, the invention will search through the downsampled sinusoidal data 14, 14' from the candidate user, to find a closest available match for at least one of

the subsets from the authorized user. The way in which the subsets are prepared for such a search, during preprocessing 58, strongly influences both (1) the data-storage requirements for the system and (2) the time which passes while the prospective user is waiting for the invention to make its decision.

A tradeoff between these two factors, data storage and real-time processing, leads to two major alternative approaches to managing the subset preprocessing. At present the limiting consideration is time; however, in the future if much higher processing speeds become available it may become desirable to instead opt for solutions that reduce storage at the expense of time. Therefore both approaches will be outlined here.

For minimum data storage, it is possible to simply save each selected subset in the original form that appears within its respective small-window portion of the template. In this case, the subsets shown as rectangles 31' in Fig. 1 may be identified on a one-to-one basis with those selected windows, although actually there are likely to be only three or four such windows.

This minimum-data-storage case is in fact an extremely important one, so that actually it is highly desirable to save each subset — and indeed the entire data set for an authorized user — in an abstracted or abbreviated form rather than in its original form. Accordingly these options are associated with one major preferred embodiment of the invention.

They are important in particular when a compact, self-contained system either must store many templates, for each one of many (e. g., a hundred) authorized users, or must read in a template from a remote data bank — or from an identification card (e. g., with magnetic strip or bar code) carried by the user. Either of these cases puts a premium on smallness of the data file for each user, since full data (and even more emphatically preprocessed full data) are very costly to store within the system for multiple users, or to transmit or store on an ID card. This first major preferred embodiment is particularly applicable in environments where a short additional delay, perhaps a half second to a second, for calculations is acceptable — automatic tellers, office doors, etc.

In later real-time processing, however, if a subset is presented for comparison only in its original form, sifting through the candidate data 14' for a particular subset is relatively unlikely to succeed. This is true even if the candidate is in fact the authorized

user, since there is a fairly strong likelihood that the subset of interest has been rotated or dilated, or both.

Therefore a fair test requires, to begin with, checking each region of the candidate data 14' against several rotated forms of the subset under test — rotated through different angles. In addition to a nonrotated subset, the preferred embodiment checks eight nonzero rotations, ranging from negative (clockwise) through positive angles.

A fair test also requires checking each such region against several dilated forms of that same subset — dilated by different factors, ranging from values below unity through values above unity. A second major preferred embodiment therefore checks, in addition to a nondilated subset, six nonunity dilations.

Furthermore each region of the candidate data 14' should be checked against forms of that subset which have been both dilated and rotated — covering most or all crosscombinations of those same rotation angles and dilation factors. Taking into account the zero-rotation, unity-dilation cases, the second major preferred embodiment of the invention preferably uses nine rotations and seven dilations, for a total of sixty-three cases to be checked.

Each case represents rotation and dilation isomorphically — that is to say, without change of shape. Each of the sixty-three variants may be termed an "isomorph".

As will be understood, for a representative three subset windows this works out to nearly two hundred isomorphs to be checked against each region of the candidate. During real-time processing all these variant forms can be constructed geometrically by the processor, but at this writing the additional time occupied in this effort — or the additional cost of parallel processors to do this work — tends to make this approach prohibitive for high-urgency applications such as weapons or emergency communication systems.

Preferably instead, for the present, each of typically three subsets is preformed (or "premassaged") into each of the sixty-three isomorphs (Fig. 2) described above, and each of the resulting one hundred eighty-nine isomorphs is stored in the apparatus. This represents the tradeoff that yields minimum processing time but maximum storage, and as pointed out just above is associated with a second major preferred embodiment; it is particularly appropriate to single-user environments (e. g., personal weapons) where extremely rapid verifications are required with very high certainties.

For a clearer conceptual grasp of the multiple-isomorph preformation technique, an original subset 31 (Fig. 2) may be regarded as at

the center of an array of several rotations (shown in the drawing as arrayed from left to right in order of increasing counterclockwise angular values) and several dilations (shown as arrayed from bottom to top in order of increasing dilation). Rotations are emphasized in the
5 illustration by radial tick marks at the four compass directions of the original.

Negative or clockwise rotations thus appear to left of the centrally placed original 31, and dilations by factors less than one — or in other words contractions — appear below that central origi-
10 nal 31. Pure rotations are in the same row directly to left and right of the central original 31, and pure dilations are in the same column above and below it.

Crosscombinations make up the remainder of the illustration, for instance an isomorph 31'm of maximum negative rotation combined with a
15 two-thirds-of-maximum positive dilation being shown near upper left. Whereas an original subset 31' (Fig. 3) is always in the original relation to its full template 21, in general it will later be found in some other relation (if at all) in the candidate data 11.

Thus the same above-introduced isomorph 31'm (Fig. 2) —
20 clockwise-rotated and rather strongly dilated — may appear in a different position in the candidate data (Fig. 3). The association of such a structure 31'm with both the template 21 and candidate data 11 thus links the two data sets together, and reveals how an isomorph 24 of the entire template 21 must be selected and disposed for a fair
25 comparison. Just such information 38 is what is sought by the global search 32-37.

As will be clear to those skilled in this field, any of a great variety of compromises may be struck. These may involve — merely by way of example — storing all the rotational variants but constructing
30 all the dilational variants on the fly, or vice versa; or storing certain of the rotational variants and constructing others as perturbations of stored ones, etc.

Thus a third major preferred embodiment is associated with a family of such tradeoffs, one tradeoff in particular involving use of
35 seven rotations and three dilations for a total of twenty-one isomorphs at each subset 31'. Another tradeoff is performing most derivations 28, 29, 22', 22'', 31 on the fly.

For the above-mentioned second major preferred embodiment illustrated rectangles 31' in Fig. 1 actually represent a considerably
40 larger number of stored variants of some three subsets or windows selected 31 from the template 21. This preparation pays off hand-

somely later, in a blindingly efficient search through the candidate data 14' for all one hundred eighty-nine isomorphs, constant-shape variants.

For maximum search efficiency it is advantageous to store the
5 Fourier transforms of the subwindows, rather than their direct spatial representations. As will be seen, this preference saves time in the real-processing stage because the procedure preferably uses the transforms.

Returning briefly to the first major preferred embodiment men-
10 tioned above: storage of templates in abstracted or abbreviated form (e. g., level-downsampled to two-bit or binary data) does require care to avoid loss of ultimate performance. I have found that such storage need not impair accuracy if the data are properly processed after retrieval.

15 In particular, routine template-data steps of bandpassing, normalizing and smoothing should be performed on the abstracted data to as nearly as feasible reconstitute the original information set. These steps beat down the high frequencies introduced by storage in one- or two-bit form.

20 Another critical time for success of such methods is preparation for storage. The raw data should be smoothed, downsampled and normalized before storage.

Selection and stepping of the comparison regions in the global
25 search — In real-time processing, the first (most distinctive) of the subsets or windows 31' is selected for comparison with the filtered candidate print 13. In Fig. 1 this function is called "subset stepper" 32.

More specifically, the stepper 32 selects a first one of the
30 sixty-three isomorphs of the first window or subset 31'. In simple spatial terms, it is desired to find a portion, a small region, of the candidate print 14' which most closely corresponds to this first subset isomorph 31'.

One straightforward way of finding that most closely correlated
35 candidate-print region would be to simply pass the first subset isomorph 31' systematically over the whole candidate print. While doing this, it would be necessary to keep a record of the quality of the match between the isomorph 31' and each portion of the candidate print traversed.

40 For example, the apparatus might first position or superimpose the first subset isomorph or variant 31' in the upper left-hand corner

of the candidate print, and measure the similarity (goodness of correlation) between the first variant 31' and the superposed candidate region. Then the apparatus would record that correlation value in association with the position. Next the first variant 31' might be
5 shifted to the right by a distance equal to some fraction of the typical ridge spacing, and the measurement and recording repeated for this new position. When the comparison process reached the right-hand edge of the candidate, the apparatus would shift the first variant 31' down by, again, a distance equal to some fraction of the typical ridge
10 spacing, and then again scan across the candidate print while recording correlation values at each position. This entire sequence would be iterated until the comparison had been completed for all rows.

From the recorded data the system could then pick the best correlation value, and retrieve the position information associated
15 with that value. The result would be a specification of both (1) the best correlation position for the first subset variant 31' and (2) the quality of the correlation there.

The scanning-and-recording procedure described to this point is closely equivalent to the mathematical procedure of convolving the
20 candidate print with the first variant subwindow. As can be seen from the above description it entails a very significant amount of processing time, though it only finds the best correlation for just one of the plausible rotations and/or dilations of the first subset.

25 With the data expressed in sinusoidal terms as previously mentioned, the same output information can be found much more efficiently by search for the correlation in Fourier space, as follows. First the Fourier transform of the candidate print is multiplied by the Fourier transform of the particular rotated, dilated subwindow of the tem-
30 plate.

The resulting product is back-transformed, yielding a real array that holds the quality of correlation for each position of interest —
i. e., for each position in the candidate print, just as if found by stepping across and down as described above. In this array, location
35 of the maximum correlation value represents position in the candidate print, and the value itself is the quality of correlation at that position.

The output array of the back-transform actually holds data that are the equivalent of spatial stepping at intervals equal to the data
40 spacings — i. e., in view of the previously mentioned periodicity-controlled downsampling 13', finer intervals than the ridge spacings.

Thus the procedure yields the best-match position of the subset in the candidate, and the quality of the match.

From a purely mathematical point of view, this two-step process might be deemed equivalent to convolving the candidate with the sub-
5 window — but, if so, only in the sense that mathematical proofs are available to show the equality of the output numbers. In practical terms (and patent terms), to the contrary, the Fourier method is not at all equivalent: the process itself is extremely different, and the result includes obtaining the desired information in a far shorter
10 time and with many fewer computer transactions or steps.

Thus this Fourier process is preferable to direct comparison of the spatial data because it is much more efficient. In preparation for this process, as mentioned earlier, the numerous subwindows of the template are preferably stored as their Fourier transforms, and the
15 candidate print too is Fourier transformed — just once, at first entry to the location-estimating stage 34.

For best results some positions in the candidate print — in other words, some values in the array — are excluded from consideration. The apparatus should not be allowed to select regions that are
20 subject to edge effects, in particular, or any other systematic major corrupting influence.

The Fourier-transform procedure itself has alternative versions. In particular, for greatest efficiency, rather than a two-dimensional Fourier transform the invention can calculate two successive trans-
25 forms of the so-called "Fast Fourier Transform" (FFT) type, one for each of the two dimensions of the candidate print.

The invention as described to this point thus finds the region 38 (Figs. 1 and 3) of the candidate print that most closely matches the
30 first subset 31' of the template, taking into account an ample range of rotations and dilations — i. e., a best-matching isomorph 31'm. In the process the invention also finds a measure of the quality 36 of that closest match 38.

If that quality is better than a preestablished threshold, the
35 invention can be programmed to conclude that the found position, orientation and dilation are clear and clean enough for use in the following procedural stages. At this early stage, the displacement, rotation and dilation thus found are assumed to have affected the entire template equally, i. e. globally.

40 In other words it is assumed here that the candidate print may have resulted from only certain kinds of changes in the template:

shift, rotation, and overall change of scale isomorphically (size change while holding constant shape). The apparatus then proceeds to use this information in an isomorphic adjustment 23, which will be discussed shortly (and which will be a prelude to the next major side
5 calculation 41-47, 25-26).

If, however, the quality 36 of the closest match 38 is not better than the preestablished acceptable quality, then it is reasonable to conclude that either (1) the candidate print was not made by the
10 authorized user or (2) operating conditions led to some disruption of the authorized user's print, particularly in the area of the first subset 31'. This second possibility must be carefully accommodated to avoid false negatives — i.e., rejection of the authorized user.

The preset threshold of quality used here need not operate
15 arbitrarily to cut off analysis, as for example in the Driscoll system. Rather, if the candidate print fails the established quality criterion here, the apparatus can be made to conclude only that perhaps the failure is just a matter of unusable data arising from local disruption of the authorized user's print. In this case the
20 system is programmed to repeat the stepper process 32, but using another subset from the original selection 31 of subsets or windows 31' in the authorized-user template 21 — in effect simply looking for usable data elsewhere in the candidate data 14'.

25 When the invention cannot find an adequate matching position in candidate data for any of the sixty-three variants of a first window, it resorts to the next most distinctive window or subset 31' previously selected. It looks for a best correlation position of dilated and/or rotated forms of that window.

30 As with the first window, the process checks numerous variants, in effect stepping across and down the candidate print with not only the second subset but also its isomorphs at each of a series of orientation angles crosscombined with a series of possible dilations. Again from the many resulting correlation measures, the best is
35 selected. It identifies the candidate region that is a closest match to the second window 31', and at the same establishes a rotation and dilation assumed to have affected the entire template.

Again if this second set of data fails the quality threshold, the system can resort to a third, and sometimes (rarely) even a fourth.
40 If usable data are found with any of these, the system proceeds to the previously mentioned isomorphic adjustment. If not, still other

levels of analysis may be used as fallbacks; however, in testing, my invention has been found to operate satisfactorily without resort to such fallbacks. In other words, the invention has been found to successfully find a usable correlation between some one of the subsets
5 31' and any input data 14' that represent a real fingertip pattern.

Although the foregoing paragraphs describe a particularly efficient and advantageous technique, various strategies may be adopted to find the best variant of the best window 31', and best matching candi-
10 date-print position. All such strategies, whether using direct spatial stepping or Fourier techniques, are within the scope of my invention and so within the sweep of certain of the appended claims.

As indicated above, if the best match to the first subset is of
15 marginal or poor quality the selector/stepper 32 will select another subset, and similarly may then select still another. This happens most typically if the candidate is an impostor. Thus processing delay is least likely to be extended when the candidate is actually the authorized user — a collateral benefit of the previously mentioned
20 operating assumption that the candidate is the authorized user.

It is possible, however, that the first subset cannot be matched to any region of the candidate print even though the candidate is authorized. This failure may perhaps be due, for example, to damage, unusually severe distortion, abrupt folding (if such folding can
25 occur) or obscuring of the skin — or a piece of dirt or a stain — in that region.

The above-described iteration of the procedure using a second distinctive region 31' is intended to deal with this exigency. Preferably the stepper 32 selects the subsets 31' in decreasing order of
30 distinctiveness, and typically the second subset is only somewhat less distinctive than the first. Therefore only a slight loss of certainty in overall result 54-57 is suffered by resort to the second subset.

If a candidate is not the authorized user, and only rarely otherwise, the stepper may proceed to try a third and successive
35 subsets 31'. Eventually the best (or most typically for an impostor the least poor) of the subset/placement combinations is selected for use, and as will be understood the subset in this case is — relatively speaking — not very distinctive.

If, to the contrary, two or more of the subsets 31' yield com-
40 parably acceptable (but both rather poor) isomorphs, my invention could try to resolve this ambiguity by repeating the procedure for

these two subsets. For this situation, however, in principle the two subsets or regions may be treated concurrently, as a unit — or, alternatively, each of the two subsets may be considered separately, but with each subset or region being enlarged by addition of an
5 immediately adjacent region.

Such operation, though well within the scope of the invention (and the sweep of certain of the appended claims), has been found unnecessary. The preferred embodiment accordingly includes no such hybrid-subset procedure.

10

Isolation and use of the best overall match: isomorphic adjustment — Eventually the stepper 32 settles on a subset-and-isomorph combination 31'm, 38 (i. e., combination of subset with location, orientation and dilation) of a single or enlarged composite region
15 that yields the best quality-of-match index 36. At this point the focus shifts from selection of the subset-and-isomorph pair to use of the isomorph alone.

Thus the iterative procedure 32-37 produces an output that is the isomorph 38 from the best subset-isomorph combination. Again, this
20 isomorph 38 represents the shift, angling and expansion of the template 21 which make the template best match the candidate 11 in the vicinity of the selected subset of template data.

As will be seen, there is a possibility that it is only in this vicinity that the template best matches the candidate. In fact, a
25 particularly advantageous aspect of the present invention is an ability — as will be fully explained below — to deal with this possibility. At this stage, however, this best-match information is all that has been assembled.

Therefore this best-estimated position/angle/scale combination 38
30 is applied 23 as a correction to the template signal 22 — forming an adjusted template 24 (cf. Figs. 1 and 3) that is more fairly comparable with the filtered candidate data 13. In short, following the global search 32-38 is an isomorphic adjustment 23.

In the isomorphic adjustment, as the name conveys, no change of
35 shape occurs — but the entire template signal 22 (i. e., the template throughout all of its regions) is shifted, cocked, and dilated or contracted, to form an isomorph 24 of the entire template 21, that matches as nearly as possible the corresponding features 38 of the candidate print as found in the selected window 31'. Again, while it
40 might be supposed that it would be reasonable to adjust or perturb the

filtered candidate data 13, 14, the philosophy of the invention is to modify 23 the template data 22 preparatory to the comparison.

Reasoning behind this philosophy may now be better appreciated: the template is relatively cleaner and clearer, and these properties
5 are reasonably well retained in its adjusted form 24. Adjustments to the candidate data 13, 14 would interact with its relative noisiness, and statistically speaking through second-order effects disturb the likelihood of a match.

The total area imaged in the candidate print 11 cannot be closely
10 controlled to match the template 21. Moreover the template is shifted, angled and dilated: when the two data fields 14, 26 are eventually overlaid for comparison some areas of each field will fall outside the other, and so be unusable.

As in all print-analysis systems, comparison will then proceed on
15 the basis of the remaining areas, those areas which coincide, or in other words what may be called the "usable" or "overlapping" data 124 (Fig. 3). In the conceptual illustration, the coarse hatching is only intended to help identify the overlap region 124, not to suggest fingerprint ridges or the like — which of course are much finer.

20

In the Driscoll and Denyer patents, very small data excerpts from template and sample are used in proceeding directly to a final decision. In the present invention, by contrast, similarly small amounts of template data 31' preferably are used, in the global search and
25 isomorphic adjustment, in a very different way — namely only to obtain an intermediate result. That result is a "once-adjusted" template 24 which is more fairly comparable with the candidate image data 11-14.

All of the overlapping data in this adjusted template 24, which
30 is to say essentially all the overlapping data in the original template 21, will eventually be used. Furthermore, all these data will be used in comparison with essentially all of the overlapping data 14 from the candidate — i. e., excepting only the data points removed 13' as redundant.

35

Demodulation, gradient search for distortion, and distortion adjustment: purpose — The isomorphic correction 23 adjusts the entire template based upon relative placement in just one small region. Therefore, even if the candidate is in fact the authorized
40 user, there still exists a crucially important potential for mismatch between the adjusted template 24 and candidate data 14. That poten-

tial resides in the possibility of twisting or other deformation in the candidate.

In other words, the candidate user's finger may have been applied to the sensor surface in such a way as to distort the overall pattern.

5 Such distortion consists of differential offsets, rotations and dilations internal to the pattern.

No single isomorphic adjustment can possibly take account of such internal differential effects. It is believed that internal distortion may be most to blame for failure to reliably verify presence of
10 an authorized user — false negatives — in even the most highly sophisticated of prior-art systems.

Again Driscoll seeks to deal with these phenomena by allowing for, and seeking, small movements of a secondary and/or tertiary
15 window relative to expected position. The system of Driscoll apparently is limited to such displacements that can be interpreted as part of an overall rotation of the print.

Driscoll does use a least-squares fit to find the best position for an overall-rotated version of his template, to use in comparison.
20 Such a fitting technique may perhaps implicitly permit other kinds of movements — isomorphic dilation or differential distortions. A least-squares fit, however, would be appropriate if departures from positions corresponding to an isomorphic rotation were merely "random" error in the larger sense of lacking correlations, lacking even soft
25 constraints.

The present invention proceeds on the basis of a much more complete statistical model than Driscoll's methodology implies. The present invention automatically applies a kind of relatively low credence, on a sliding scale, to information that has a relatively
30 high degree of inconsistency — but without entirely discarding such information.

Although some uncorrelated measurement error may be present, there is no basis for assuming that the entire amount of departures from predicted positions are without mutual correlation. Different
35 portions of fingertips are not understood to undergo relative displacements that are uncorrelated.

To the contrary, different portions of fingertips are understood to be physically interconnected by skin and flesh, interrelated through their interactions with skeletal members, and otherwise
40 coordinated systematically. Furthermore the use of a least-squares fit, being divergent from the reality of skin-pattern internal rela-

tionships, cannot provide meaningful guidance for either assessing or limiting the character or magnitude of relative movements other than those found through isomorphic rotation.

The Denyer patent too speaks in very general terms of making allowance for such movements. It offers little or no guidance as to how such allowance might be made.

What both these prior systems fail to provide is any systematic or principled theoretical basis, for constraining the amount of "allowance" for these movements that is permitted. This failing is crucial, for inadequate "allowance" will result in turning away an authorized user, but given enough unfettered "allowance" almost any print will match almost any other.

Of course some experience may be brought to bear in making an educated guess about amounts of rotation or twisting that seem plausible, and amounts that seem too permissive and thus too likely to grant access to impostors. The measurement space in which such prior-art guesses must be made, however, appears very ad hoc or addressed to a particular physical immediacy — essentially a form of designing at the drill press.

The proper extent of such "allowance" is therefore not readily amenable to quantification or to statistical analysis, and this fundamental limitation aggravates the previously noted limitation of making final decisions based on a small fraction of the available information. As will be seen the present invention, by contrast, is able to relate the amount of solidly expected variation — through direct application 18, 18' of the a priori statistics 17 — to the measurement preparations 44 and final-decision preparations 52.

The assessment and use of this sometimes-so-called "prior portion" 17 of the expected signal statistics advantageously tend to favor smoothness in the distortion field as estimated. The prior statistics rest on an implicit assumption that the distortion field contains some correlation structure — some physically based interrelationship between what happens in one part of the field and what happens in another.

As noted above, different portions of the skin pattern are, after all, physically interconnected — each part pulls on each other part (and that "other part" pulls back). The prior statistics thus quantify the degree to which individual displacements (which in the aggregate constitute the distortion field) are correlated with each other. Preferably a Fourier-space model is used for the prior-portion statistics 17.

With some of the hardest work done in the global search 32-38 and isomorphic adjustment 23, my invention is now able to very efficiently isolate 42-47 and adjust 25 (cf. Figs. 1 and 4) the template for distortion. In a very rough conceptualization, this is accomplished
5 by applying 25 (Fig. 4) the distortion field 45 to the once-adjusted template 24, to obtain a distortion-corrected template field 26.

The distortion field 45 (Fig. 4) also is roughly conceptualized as a field of displacements 45a, for example moving fixed vertical grid lines 45" (symbolizing the structure of the frame of reference
10 itself, i. e. the web of the skin as distinguished from its pattern of ridges and troughs) to left or right so that the grid lines 45" assume new forms 45b. Arrowheads 45a representing the individual displacements are in many portions of the drawing very short, and so can be seen as only very small arrowhead tips.

15 The distortion field 45, 45a has been drawn very simplified: there are no displacements of the horizontal grid lines 45'. The drawing does show, however, that on balance the overall amount of leftward and rightward shifting is about equal — as it should be, since any isomorphic dilation or contraction should have already been
20 incorporated into the isomorphic adjustment 23 which formed the first-adjusted template 24.

The symbol "*" in Fig. 4 is not to be misinterpreted literally as an actual multiplication: though some complex multiplication is involved, that would be an oversimplification; rather the symbolism of
25 multiplication is only intended at a rough conceptual-analogue level to represent application of a distortion field 45. The distortion-corrected field 26 will later be used as a matched filter in the final comparison 51. To extract 42-44 the distortion 45 and so prepare the data for this nonisomorphic adjustment 25, I first treat the distortion
30 45 as if it were a data signal impressed upon a carrier wave — in other words, as if the distortion were a relatively slowly-varying information signal modulating a carrier.

The carrier in this situation is the relatively higher-spatial-frequency ridge/groove pattern of the natural fingerprint, with the
35 finger at rest or undisturbed by differential stresses. Two clarifications are needed:

First, it must be recognized that in the final analysis, literally the final analysis 51-56, what is of interest is the ridge/groove pattern rather than the distortion. The focus upon the distortion at
40 this point is only temporary and only for purposes of isolating and

then canceling it — just as the global search isolated placement/dilation so that it could be globally (but isomorphically) canceled.

Second, not only the distortion but also the "instantaneous carrier" (local harmonic content of the ridge/groove pattern) varies strongly from place to place within the candidate image 13. Hence it must be understood that distortion will necessarily be extracted as a vector field, varying over the image area, not a single global parameter and not even a scalar field — and the "carrier" too must be treated as a field with many strong local variations.

10

Obtaining a "carrier" for use in demodulation — Fortunately it is unnecessary to determine what this varying carrier field is, in a candidate image 13. Instead the authorized-user template 21 is taken to be the carrier for the candidate data.

15

Properties or characteristics of the template 21 needed to implement this approach can be found in advance, during preprocessing 58. Part of this is done by in effect mapping 28 the local ridge spacings and orientations, and saving the resulting magnitudes and directions as vector wavenumber fields 29.

20

Here too the assumption that the candidate is the authorized user is put to major advantage: the template 21 is assumed to be the carrier of a distortion field, a vector field, in the candidate 11, 13. The vector wavenumber fields 29 of the template represent the spatial frequencies of that carrier.

25

Once again, if the candidate is not the authorized user, these latter assumptions fundamentally become gibberish and the ensuing correlation most commonly fails dramatically.

Demodulation of the distortion field — My invention next proceeds to actually estimate directly, in three steps 42-44, the entire distortion field 45. The first step 42 is demodulation to obtain an intermediate result, namely a complex field whose phase is sensitive to an assumed vector distortion field.

For this purpose, forms 41, 41' of the template 21 are needed that contain information about both the ridge locations (with their spacings) and their orientations. Stated first simply, multiplying the template form(s) 41, 41' and candidate data 14" together yields the desired intermediate field 45.

The original template 21 (as well as the once-adjusted template 24) taken by itself is passed 41 to the demodulation process 42, but lacks phase data that are needed for such a procedure. Therefore I

begin by constructing somewhat synthetic forms 41" of the template that include phase information.

More specifically, the template 21 (carrier) is first expressed in a modified form, which is obtained through multiplication of its spatial gradient field 22' by its own vector wavenumber field 29:

$$(\text{quadrature form}) = \frac{(\text{template gradient}) \cdot (\text{wavenumber field})}{(\text{wavenumber})^2}$$

This preliminary product represents a scalar 22" that is in quadrature with the template.

By the phrase "in quadrature" I mean 90° out of phase, or using radian angular measure $\pi/2$ out of phase. In other words the scalar 22" found by this multiplication process is everywhere in the pattern inherently one quarter of a spatial wavelength offset from the basic template. The denominator normalizes the expression; thus the quadrature form differs only as to phase, not as to amplitude.

It is known that a quadrature form of a periodic positional signal, used in conjunction with the basic positional signal itself, can yield directional or phase information for use by automatic apparatus in determining, for example, a direction of motion. In my invention a like underlying principle is used, albeit in a conceptually very remote context, to enable the algorithm to keep track of the direction in which features of the candidate print are offset from features of the template.

If not for the reentrant character of most skin patterns of interest, it would be sufficient to use a quadrature form 22" of the template in just one single version. The typical closed patterns 62 (Fig. 2) and whorls familiar in fingerprints, however, render such a simple representation inadequate for the following reasons.

In a generally linear region 61 of a print, of course if one could monitor, along a path very generally from ridge 75 to ridge 75', it would be natural to expect continuity of phase-gradient direction 65, 65' — i. e., the direction locally perpendicular to each ridge-line, in which phase increases. By the phrase "continuity of phase-gradient direction" here is meant the property of the direction being consistent, or in other words not reversing (except perhaps where it is near zero).

Such continuity as illustrated by phase-direction arrows 65, 65' near the left end of the drawing, is expected irrespective of the fact that two adjacent, parallel ridges 75, 75' happen to open up into a

whorl 62, and as shown even a whorl which includes distinctly closed loops.

The phase-gradient directions 65, 65' for both such adjacent parallel ridges 75, 75' — which happen to span such an enlargement 66 —
5 can be traced toward the right along the respective ridges 75, 75'. Eventually a point 72 is reached at which the "two" ridges 75, 75' are found to have been actually different tails of just one common ridge 75-75'.

At some such place along the way, therefore, the initially common
10 phase-gradient directions 65, 65' are found to be directed oppositely 68, 68'. If this phenomenon is not somehow controlled, the entire phase field becomes unmanageably ambiguous as can be seen by tracing the upward-pointing phase arrows 65 around the loop.

Such tracing finds likewise upward-pointing arrows 67 across the
15 top of the whorl 62, rightward pointing arrows 68 along the right end 64 of the pattern, and downward-pointing arrows 69 back across the bottom to the left end 61. Even in this latter region 61 of generally parallel and rectilinear ridges 75, 75' the downward arrows 69 are oppositely directed from not only the upper set of phase arrows 65
20 above the division line 66 but also the lower set 65'. That lower set, as will be recalled, is associated with the identical ridge line 75' below the division line.

To deal with such potentially troublesome discontinuities, my invention forms not just one but at least two quadrature forms 22" of
25 the previously discussed gradient-times-wavenumber product — which is a scalar. Furthermore in operation the algorithm of my invention must automatically select a particular one of the plural quadrature forms for use.

Preferred embodiments of my invention make this selection based
30 upon monitoring for phase discontinuities of the sort illustrated. The monitoring is preferably carried out by detection of sudden reversals in sign of the wavenumber field 29.

These sign reversals can be found during preprocessing 58, and their locations marked by warning flags 73, 74 a specified distance
35 from each discontinuity 72 — in each direction along an axis transverse to the discontinuity. Preferably this work is done during preprocessing, in formation of the template, moving one step at a time in either the x or y direction, in real space — while requiring neighboring values to be substantially continuous, and setting up the
40 flagging in an associated wavenumber field 29. In terms of the Fig. 2 example, continuous processing along a vertical (y) direction locates

the discontinuity 71 at a height 72 in the pattern. Later in actual candidate processing, with the wavenumber field downsampled 43 onto the coarsest grid, the system watches for the flags 73, 74 only at right angles to the direction y selected previously for imposition of continuity. This strategy enables the processing to stay some distance away from a discontinuity.

For computational convenience I express the template 21 as a complex number. I set the real part of this number equal to the direct spatial form of the template 21, 22, and the imaginary part equal to the selected one of the preliminary products, the in-quadrature scalars 22", just described, i. e.:

$$\text{template}' = \text{template} + i \cdot (\text{quadrature form of template}),$$

where i is the base of imaginary numbers, the square root of negative one.

Both the real 22 and imaginary 22" parts of this variable are then subjected in real processing time to the isomorphic adjustment 23. The adjusted results 24, 24' are passed 41, 41', as already suggested, to the demodulation process 42.

Here the complex variable template' as mentioned above is multiplied by the candidate data 14", yielding a new complex variable in which is embedded phase information related to the distortion field that is being sought. The distortion field in fact is fundamentally a phase-displacement field, though in some minority of cases the phase shifts due to distortion exceed a half-wave (180° , or π radians) and even a whole wave (360° , or 2π radians).

The cases in which maximum distortion thus exceeds half of a ridge spacing, although ordinarily in the distinct minority, are by no means negligible. To the contrary they are extremely important in successful practice of my invention. I have found experimentally that if such cases are neglected the resulting ambiguity of displacement direction — and gross errors in implied character of the candidate print — are often catastrophic to recognition of the authorized user.

The new complex variable resulting from this demodulation (multiplication) step may be represented so:

$$\exp \{ i \cdot (\text{distortion field}) \cdot (\text{wavenumber field}) \} + \text{noise},$$

in which "exp" means the exponential function, and "distortion field" is the unknown random field 45 quantified statistically by the a priori data 17.

The factor "wavenumber field" represents the same known vector
5 wavenumber field 29' used earlier in constructing the quadrature form of the template. The additive term designated "noise" corresponds to the residual effects of all features of the candidate data that do not represent the local sinusoid associated with the ridges and troughs of the candidate user's skin pattern. The immediate object of the in-
10 quiry is to determine the distortion field. As can be seen, the "noise" term obscures the desired answer.

If one wishes to find the true answer it is very desirable to at least make some allowance for the full expression, including the "noise" term, presented just previously — since that full expression
15 is the quantity which has been found through the demodulation process. The preferred embodiment does make allowance for the measurement noise by downweighting the demodulation locally, in general proportion to local noisiness in the data — or, in other words, by discounting information from regions known to be noisy.

20 Of course it would be much easier, in a manner of speaking, to simply use a "fitted" phase without regard to any distortion field or wavenumber field — that is to say, a phase which appears to account for observed mismatches between template and candidate, but is not too large. Doing so, however, would be in a sense somewhat analogous to
25 the "allowing" of some plausible amount of translational wandering or rotation in the Driscoll method discussed earlier. It would be very hard to say, based upon any reasoning from first principles, how to constrain such a fitting, or in other words just what "not too large" means. This is analogous to the problem noted earlier, relative to
30 the Driscoll system, of establishing how much translation or rotation is plausible and how much is simply letting in more candidate users.

One of the particular benefits of the present invention is that it enables estimation of an actual distortion field that is consistent with (1) the assumption that the candidate user is the authorized
35 user, and (2) a term "noise" that corresponds to measurement noise in the candidate data, and (3) an additional noise term representing a magnitude and degree of smoothness, in the distortion, which is not only plausible and not only "not too large" but actually statistically likely as quantified in relation to the a priori statistics.

40 Thus by approaching the phase-field or distortion-field determination from this seemingly roundabout direction the present invention

places the relevant relationships in a form that is amenable to direct use of known variabilities in fingerprint placement. The entire verification process is thereby placed on a footing which is far more solid and physically meaningful than ever possible heretofore.

6 It remains, however, to say how the distribution field can be extracted from the expression presented above. This is by no means a trivial exercise, as it calls for, in effect, inverting a matrix which is multidimensional — more specifically, having as many dimensions as there are downsampled 43 data points to be used.

10

Downsampling for tractable processing — Thus extraction of the distortion field involves extremely intensive processing. If it were necessary to perform such procedures at full resolution, which is to say on the entire received data set 14" after the first downsampling
15 13', the required processing time would be prohibitive in most routine uses. With present-day limitations of processing speed it can only be rendered feasible through a two-part "smoothing and second downsampling" stage 43. Of the two parts of this stage 43, the one that may be regarded as the more fundamental is the second downsampling, to
20 reduce by an additional large factor the amount of data to be thus intensively processed.

The earlier downsampling 13' was justified on the basis that the data was represented in periodic terms, and that use of sampling intervals much smaller than the smallest period represented in the
25 template could only produce redundant data. Like reasoning applies to the distortion field, but the latter is assumed to change far more slowly — an order of magnitude more slowly — than the elevation changes corresponding to the basic ridge-and-groove pattern.

Fortunately the desired distortion field as a practical matter is
30 almost always a relatively smooth pattern. It is most typically a differential dilation — such as may be expected from pressing some parts of a fingertip more forcefully than others.

In some cases it may also, or instead, partake of a relatively gentle twisting, such as a "C" or sometimes "S" curve — and much more
35 rarely with an abrupt near-discontinuity, such as mentioned above in connection with the need to resort to second or third local subsets
31' in the global search.

Consequently a much smaller amount of candidate data, sampled systematically from the filtered candidate data 14, 14" after demodulation
40 suffices to define the distortion field. Thus it is again

reasonable to eliminate merely redundant data by downsampling 43 to a much longer sampling interval than used in the first downsampling 13'.

In the very occasional case of a considerably more abrupt form of distortion, just mentioned, the distortion is so abrupt that it can be treated as an entirely different case — a near-discontinuity, e. g. a very severe local distortion of the skin in a particular region.

As indicated previously, however, my invention can deal successfully with such cases. It first avoids them in selection of template subsets 31' for the global search; and it later successfully matches other very large areas of the print, in the final comparison 51.

This is a major advantage of the use of essentially all available data, data drawn from an entire print — as mentioned earlier — rather than only isolated regions. Earlier systems, even relatively sophisticated ones such as Driscoll's and Denyer's, typically are quite unable to verify an authorized user when one or more of the most distinctive regions happen to be disturbed in this way.

In this second downsampling it is permissible either to down-sample from the first downsampled data 14 as illustrated, or to down-sample from the fuller data set 13. The former, however, will be much faster. In choosing the second downsampling interval, care should be taken to avoid inadvertently, implicitly limiting the degree and character — e. g., abruptness — of distortion taken to be present. Arbitrary limitation without physical basis can skew the results.

Limits on distortion should arise from the model in use — specifically, by downsampling at sampling intervals which are related to a measure of the local rate of relative change of phase in the data. This measure conveniently should correspond to the highest significant spatial frequencies in typical or representative distortion fields for real cases.

Such information is contained in the statistical a priori data 17. Therefore, to obtain such a measure, the preferred embodiment first extracts from the a priori statistics 17 an estimate 18" of the power spectral density for distortion fields generally (in other words, not from the candidate data 11 or template 21). It then sets the sampling intervals, as a function of position, in accordance with that estimate 18" of power spectral density.

Bandpassing was used in preparation for the first downsampling 13' — not only for control of noise as such but also specifically to

avoid downsampling to nonrepresentative data points. Similarly it is desirable to smooth the data before the downsampling procedure.

This smoothing is the other, and perhaps the less fundamental, of the two parts of the "smoothing and downsampling" stage 43 mentioned
5 above. In the preferred embodiment it is implemented as a low-pass (Fourier) filter — realized with Fast Fourier Transforms. Preferably the smoothing is done as a convolution — with a fixed window in Fourier space — in close conjunction with the second downsampling.

10 Estimation of the distortion field: gradient search — My invention here uses once again an approach that depends upon manipulation of the overall pattern. Here the pattern is considered as a matrix, and the best-fit distortion field is sought by an iterative approach. This approach in effect tests the improvement in fit found by initial-
15 ly assuming a distortion field, sequentially making many small changes in that field — at each point assessing the results in terms of quality of fit — and then redirecting subsequent changes accordingly. At each point the assumed field is modified in a direction which the processing results up to that point suggest will further improve the fit.

20 This iterative approach is somewhat akin to finding the summit of a hill by probing at each point for an uphill slope, and then following it uphill a short distance to the next test point. In fact the gradient of a quality-of-fit function is used in this process. The "gradient search" 44 used in my invention, however, is multidimension-
25 al. In other words the "hill" is assumed to be a peak in quality-of-fit space, and this space has a number of "dimensions" equal to the number of data points in use — in other words, even after the downsampling described above, typically some thousands of dimensions.

In the progressive approach to finding the best fit, it is
30 crucial to avoid taking individual steps that are too large. Apart from the relatively straightforward hazard of overshooting the peak (which can be correctable in later steps if they are not too large), a much more insidious kind of error arises from excessively long steps.

As mentioned earlier, many realizations of skin patterns are
35 subject to distortions which amount, locally, to more than a half wavelength or even one or more full wavelengths in the pattern. If such a distortion is allowed to develop too rapidly, the only portion of it which is in effect "visible" is the fractional part remaining after deduction of an integral number of wavelengths.

40 It is essential to realize that correlation goes to zero in any region of the template that is misaligned by only a quarter of a

wavelength. Hence, avoiding errors of a half wavelength, or of course anything larger than that, is of extremely great importance to successful practice of my invention — at least in those cases where sizable distortions are in fact present.

5 Scaling of the steps to avoid falling into such ambiguities is best achieved by limiting the algorithm's propagation rate in the spatial or frequency domain, preferably both, outward from the initially small region of close match ensured by the global search 32-37. Thus search 44 for an estimation of the distortion field begins in a tightly
10 defined region about a distinctive point in the template and is allowed to expand slowly stepwise. Permissible expansion rate depends on ability to extrapolate judiciously from previous distortions. Preferably the expansion or extrapolation steps are related to intervals previously established for use in the second downsampling 43.

15 Computational burdens in the gradient search are borne by Fast Fourier Transforms, which are very efficient. The procedure continues until the window has expanded to the whole field.

Isolation and use of the distortion field — The iterations of
20 the gradient search 44 lead to definition of an estimated distortion field 45. This field 45 next is subjected to an intermediate upsampling step 46, through interpolation — preparatory to use in a distortional or nonisomorphic adjustment 25. This distortional adjustment 25 will form a twice-adjusted template 26, which should provide
25 the fairest possible final comparison 51 with the candidate data 14.

The intermediate upsampling step 46 is needed because the distortion field 45 was developed on a very coarse grid due to the second downsampling 43, but the twice-adjusted template 26 must be available
30 at full resolution. It is needed at generally the same sampling as established on the candidate-data side in the first downsampling 13'.

Accordingly, what is read out to the distortion-adjustment step 25 is an upsampled version 47 of the field 45; it is this upsampled version 47 which is applied 25 to the once-adjusted template 24. The application 25 step is done by multiplying together the two complex-
35 valued fields template 24 and $\exp \{i (\text{distortion field}) \cdot (\text{wavenumber field})\}$, and retaining only the real part of the result.

The resulting twice-adjusted template 26 should provide the best possible likelihood of a match with the candidate data 14 — if the candidate is in fact the authorized user. If not, then as suggested
40 earlier the greatest likelihood is that the twice-adjusted template 26 will bear little relation to the candidate data 14.

Final comparison, thresholding and decision — The twice-adjusted template 26 and the once-downsampled candidate data 14 are then compared 51. This is done by multiplying them together and summing over
5 the image, subject to inverse weighting 16 based on the candidate-image noise variance estimates 15. In this process the twice-adjusted template 26, with the associated twice-adjusted quadrature forms 26' and twice-adjusted wavenumber field 29", constitute and are used as a matched filter. The result of the filter process 51 is used to form a
10 major part of the test statistic 52.

The latter is preferably formed according to the Neyman-Pierson analysis as a ratio of the likelihoods of occurrence of the processed candidate print data according to two contrary hypotheses — namely, that the authorized user (1) was and (2) was not the maker of the can-
15 didate print. Based on this "likelihood-ratio" procedure, the above-mentioned test statistic 52 also incorporates noise statistics 18, once again providing an opportunity to ground the results in solid reality by applying the a priori statistics 17 for the distortion field.

(As a practical matter, for easier management of ratios spanning
20 a very large range of values I prefer to employ the logarithm of the ratio. This variant is sometimes called a "log-likelihood-ratio" method, in turn familiarly abbreviated to "log-likelihood" method.)

As explained earlier, these data are "a priori" in the sense of not being derived from either the candidate print or the authorized-
25 user template. They are not, however, "a priori" in the sense of being derived from first principles; rather, these data are collected empirically. (In particular there appears no indication that Driscoll takes into account any such considerations as the a priori term.)

One particularly beneficial property of the Neyman-Pierson ap-
30 proach is that assessment of the two above-mentioned contrary likelihoods is straightforward. These correspond rather directly to the probabilities of false negatives and false positives, respectively.

In a representative Neyman-Pierson diagram, not particularly associated with the present invention, a composite test statistic T
35 (Fig. 6) represents a log-likelihood parameter such as mentioned above. The two generally bell-shaped curves 81, 82 at left and right represent the probabilities of two mutually inconsistent hypotheses.

To relate this graph to the general field of fingerprint verification, for example, the curves 81, 82 might represent the probabili-
40 ties that a particular print was formed by, respectively, an impostor and the authorized user. A diagram of this sort depends strongly on

many different experimental facts, particularly including the amount of noise or experimental error in the system.

The vertical line near the intersection of the two curves represents selection of a particular threshold value T_r of the test statistic T . The shaded area 83 extending leftward from that line, under the left end or tail of the right-hand curve 82, represents the probability of a false rejection of the authorized user — or in other words, as it is sometimes called, a "type 1" error.

The shaded area 84 extending rightward from that same vertical line T_r , under the right end or tail of the left-hand curve 81, represents the accumulated probability of an erroneous acceptance of an impostor — a false acceptance, or a "type 2" error. As will be apparent, the relative sizes of these two types of errors can be adjusted by sliding the threshold or discriminator T_r to left or right.

This very general diagram is characteristic of a great many kinds of processes, and as can be seen the two areas 83, 84 representing erroneous decisions each are here arbitrarily drawn as amounting to a few percent, perhaps as many as eight or ten percent, of the respective overall areas 85, 86 under the two curves 81, 82. That general range of numbers appears to be representative of, or perhaps better than, the state of the art in automatic fingerprint verification apparatus and methods heretofore.

My invention enables both evaluation and quantitative control of these two kinds of undesirable result 83, 84 quite readily. As a result of preliminary work — with expectably some further improvement yet to be made — the overlap region 83' + 84' (Fig. 7) between the two probability distributions 81', 82' is reduced to a small fraction of one percent.

In relation to the present invention, the test statistic T can now be identified with the like-entitled block 52 in Fig. 1 (see at right in Fig. 7), and the selected threshold T_r similarly identified with the threshold 53 of Fig. 1 (see at center in Fig. 7). As will be recalled, the desired-certainty threshold 27 is set during preprocessing 58 to accord with the authorized user's preferences as to type of error least acceptable, and quantitatively that user's preferred relative balance or tradeoff between magnitudes of the two error types.

Improvement due to my invention is so great that it would be difficult to draw the two entire curves 81', 82' at such a scale that the overlap regions 83', 84' could be clearly seen in the same view (as the corresponding much larger regions 83, 84 are seen in Fig. 6).

Characteristic error probabilities 83', 84' with my invention as developed at this writing are very roughly 0.001, or one-tenth percent.

At worst, with the test statistic threshold T_r set at an optimum point within the overlap region either the false-negative or false-
5 positive rate may be a maximum of that same fraction of one percent. If the test statistic T_r is offset from that optimum point, however, then the particular kind of error of greatest concern to the authorized user can be made much smaller than that fraction of a percent.

For instance, the threshold T_r can be set well above the absolute
10 optimum point, in response to a decision by the authorized user to favor false negatives 83' (as for example to give particularly high protection against improper use by family members). The probability of a false positive 84' is thereby easily made a much smaller fraction of one percent, for example 0.01 percent, at the cost of, say, a one-
15 percent incidence of false negatives 83'.

Almost as important as the low value of the false-negative and false-positive probabilities at their crossover point is the fact that this crossover probability can be specified. In fact probability of a false positive for any particular setting of the threshold 53 can be
20 quantitatively specified, as can the associated probability of a false negative. Given such information, correlated with the range of settings of the threshold 53, the authorized user is for the first time able to make a fully informed and so at least potentially intelligent choice of the desired threshold 27. Although the relationship between
25 selected threshold 27 and actual probabilities, or actual level of desired certainty, is not direct in the sense of a linear or simple mathematical function, that relationship is both monotonic and readily stated in terms of a calibration scale or a tabulation.

30 Utilization — In operation a candidate user's finger or toe 90 — or palm, or any other surface having a comparable skin pattern — is applied to the sensitive surface 91 of a sensor module 92 (Fig. 8). The system may be programmed to start when a skin pattern is thus applied 57 (see Fig. 1, bottom left) to the sensitive surface, or if
35 desired may be provided with a separate start-up switch (not shown).

The sensor module 92 develops an electronic image 11 (see also Fig. 1). That unit 92 advantageously may be an optical detector array — e.g., one of the types described in the patent documents mentioned earlier — or any other type that yields a suitable candidate-user im-
40 age data set 11, for instance a capacitive, variable-resistance, or ultrasonic detector. I prefer to use an optical-fiber prism as de-

scribed in those documents. In view of the current economics of large sensors and optical-fiber tapers I currently prefer to use a relay lens (rather than a taper) to focus the image from the output end of that prism onto a small sensor.

5 Associated with the sensor module is a read-only memory or ROM (or a programmable ROM, EPROM) 93, which holds the authorized user's template 21, 22 (Fig. 1) and associated data 22", 29 — as well as the desired-certainty threshold 27 and the a priori statistics 17. (In Fig. 8 these several callouts are abbreviated "21 &c.")

10 The candidate data 11, template data 21, and related data sets all flow to a programmed or programmable microprocessor or "central processing unit" (CPU) 94. Stored in the ROM 93 or in the CPU 94, or partly in each, is the program described in this patent document.

The portions 91-94 of the apparatus discussed so far — and cer-
15 tain other portions if desired — are advantageously made self-contained and for certain applications also made portable. Accordingly a battery or other portable power supply 95 may be included with the sensor module 92, ROM 93 and CPU 94, and interconnections incorporated, all within a housing 96. In such a case the output enablement
20 signal 55e (also see Fig. 1) might be the only output from the apparatus. That output passes to access-control module 97, which may include a suitable local or remote switching device for passing an actuation signal 98 to utilization means 99.

The utilization means 99 represent a facility, apparatus, means
25 for providing a financial service, and/or means for providing or receiving information. Merely by way of example, and without any intent to limit types of devices which can be controlled this way, utilization means may be and/or may include a cabinet, home, office, military or other government installation, educational institution, weapon,
30 computer, vehicle ignition and/or entry, automatic teller, credit system, time-and-attendance system, or database information service.

As shown the self-contained unit 96 may provide an enablement or decisional signal 55e to a discrete access-control unit 97. In many
35 systems, however, the access-control module 97 is preferably integrated into the self-contained unit 96 — in accordance with security-enhancing integration principles described in the aforementioned document of Bowker and Lubard. Similarly the whole of the print-verifying and access-control devices 96, 97 is advantageously integrated into the utilization means 99.

40 In both cases an object of such integration is to make security aspects of print-verifying control relatively invulnerable to bypass-

ing. That is to say, integration of the whole system can provide resistance to insertion of a jumper, short, or other form of injected simulated access-control signal 98 at the utilization-means 99 input.

Thus for instance in a weapon, bidirectional information flow
5 between the CPU 94 and a detonator 99 within each projectile (bullet etc.) can prevent tampering with the intermediate firing mechanism. In a vehicle that has a distributor or other ignition module 94 directly associated with the combustion system, automatic exchange of information between the CPU 94 and that ignition module can deter
10 bypassing of the security system.

In a credit, time-and-attendance, or information-dispensing database-access system, similarly, the CPU 94 should be programmed to participate in a dialog with the central computer 94 of the credit etc. system. Such a dialog ideally is conditioned to verify not only
15 the identity of the user but also the integrity of the connection between the CPU 94 and the central system.

In view of the foregoing, further examples will now occur to those skilled in the art.

20 It will be understood that the foregoing disclosure is intended to be merely exemplary, and not to limit the scope of the invention — which is to be determined by reference to the appended claims.

WHAT IS CLAIMED IS:

1. Apparatus for verifying the identity of a person by comparing test data representing a two-dimensional test image of that person's skin-pattern print with reference data derived from a two-dimensional reference skin-pattern print image obtained during a prior enrollment
5 procedure, said apparatus comprising:
 - means for extracting from the test data an estimate of noise variance in the test data as a function of position in the test image;
 - means for comparing portions of the test and reference data, for corresponding positions in the two images;
 - 10 means for weighting the importance of comparison for each portion, in accordance with the noise-variance estimate for the corresponding position; and
 - means, responsive to the weighting means, for making an identity-verification decision.

2. Apparatus for verifying the identity of a person by comparing test data representing a two-dimensional test image of that person's skin-pattern print with reference data derived from a two-dimensional reference skin-pattern print image obtained during a prior enrollment
5 procedure, said apparatus comprising:
 - means for deriving from the test data corresponding multilevel test data that are bandpassed and normalized;
 - means for comparing portions of the bandpassed and normalized multilevel test data with the reference data; and
 - 10 means, responsive to the comparing means, for making an identity-verification decision.

3. The apparatus of claim 2, further comprising:
 - means for preparing the reference data for storage or export, said preparing means comprising:
 - means for at least downsampling and normalizing the reference
5 data, and then expressing the thus-prepared reference data in two- or one-bit form before storage or export.

4. The apparatus of claim 3, further comprising:
means for extracting the reference data from storage or from an imported data set for use in verification, said extracting means comprising:
- 5 means for bandpassing, normalizing and smoothing the stored or imported data before use in verification.
5. Apparatus for verifying the identity of a person by comparing test data representing a two-dimensional test image of that person's skin-pattern print with reference data derived from a two-dimensional reference skin-pattern print image obtained during a prior enrollment
- 5 procedure, said apparatus comprising:
means for expressing the test data in the form of local sinusoids;
means for expressing the reference data in the form of local sinusoids;
- 10 means for comparing portions of the sinusoidally expressed test data with the sinusoidally expressed reference data; and
means, responsive to the comparing means, for making an identity-verification decision.
6. The apparatus of claim 5, further comprising:
means for deriving from the reference data a map of ridge spacing and direction, and for storing the map as one or more vector wave-number fields; and
- 5 wherein the comparing means comprise means for using the vector wavenumber fields to refine said comparing; and
means, responsive to the comparing means, for making an identity-verification decision.

7. Apparatus for verifying the identity of a person by comparing test data representing a two-dimensional test image of that person's skin-pattern print with reference data derived from a two-dimensional reference skin-pattern print image obtained during a prior enrollment
5 procedure, said apparatus comprising:

means for deriving from the reference data a map of ridge spacing and direction, and for storing the map as one or more vector wavenumber fields;

means for comparing portions of the test data with the reference
10 data, said comparing means comprising means for using the vector wavenumber fields to refine said comparing; and

means, responsive to the comparing means, for making an identity-verification decision.

8. Apparatus for verifying the identity of a person by comparing test data representing a two-dimensional test image of that person's skin-pattern print with reference data derived from one or more two-dimensional reference skin-pattern print images obtained during a
5 prior enrollment procedure; said apparatus being for use in the presence of an assumed dilation of the test image relative to the reference image; said apparatus comprising:

means for estimating the assumed dilation of the test image relative to a reference image;

10 means for comparing the test data with the reference data, taking into account the estimated dilation; and

means, responsive to the comparing means, for making an identity-verification decision.

9. The apparatus of claim 8:

further comprising means for extracting from the reference data a subset thereof; and

wherein the estimating means comprise means for trial-matching
5 the subset of the reference data with successive portions of the test data, to find a portion of the test data that best fits the reference data subset.

10. The apparatus of claim 9:
wherein the estimating means further comprise means for taking possible dilation into account in gauging the test data portions against the reference-data subset, to determine relative dilation;
5 further comprising means for applying the determined dilation to roughly equalize the test and reference data with respect to the assumed dilation; and
wherein the comparing means compare the test and reference data after said rough equalization.
11. The apparatus of claim 8, wherein:
the extracting means comprise means for extracting from the reference data plural subsets thereof; and
the estimating means comprise means for trial-matching each of
5 plural subsets of the reference data with successive portions of the test data.
12. The apparatus of any of claims 1 through 11, further comprising:
sensor means for acquiring such test data; and
means, responsive to the decision-making means, for operating a switch.
13. The apparatus of claim 8, particularly for use in controlling access to utilization means consisting of facilities, equipment, a financial service, or a source or reception of information; said apparatus being in further combination with:
5 means for receiving said test data from a sensor that acquires surface-relief data from a relieved surface such as a finger;
means, responsive to the decision-making means, for applying the identity-verification decision to control access to such utilization means.

14. A secured system incorporating the apparatus of claim 13 and subject to access control based upon surface-relief data from a relieved surface such as a finger; said system comprising:

utilization means, susceptible to misuse in the absence of a particular such relieved surface that is related to an authorized user, said utilization means being selected from the group consisting of:

a facility,

apparatus,

10 means for providing a financial service, and

means for providing or receiving information.

15. Apparatus for verifying the identity of a person by comparing test data representing a two-dimensional test image of that person's skin-pattern print with reference data derived from a two-dimensional reference skin-pattern print image obtained during a prior enrollment procedure; said apparatus being for use in the presence of an assumed distortion of the test image relative to the reference image; and said apparatus comprising:

means for estimating the assumed distortion of the test image relative to a reference image;

10 means for comparing the test data with the reference data, taking into account the estimated distortion; and

means responsive to the comparing means for making an identity-verification decision.

16. The apparatus of claim 15:

further comprising means for applying the estimated distortion to approximately equalize the test and reference data with respect to the assumed distortion; and

6 wherein the comparing means compare the thus-approximately-equalized test and reference data.

17. The apparatus of claim 16, wherein:

the applying and comparing means comprise means for using the estimated distortion to generate a matched filter for use in forming a test statistic.

18. The apparatus of claim 15:
further comprising means for extracting from the test data an estimate of noise variance in the test data as a function of position in the test image; and
5 wherein the estimating means and the comparing means perform said estimating and said comparing, respectively, as a function of position;
wherein the estimating means or the comparing means, or both, comprise means for taking into account the estimated noise variance.
19. The apparatus of claim 18, wherein the taking-into-account means comprise:
means for weighting the importance of the estimating or comparing, or both, as a function of position in accordance with the noise-
5 variance estimate for the corresponding position.
20. The apparatus of claim 15, wherein:
the estimating means comprise means for using a maximum-likelihood method to estimate the distortion field.
21. The apparatus of claim 20, wherein:
said estimating means further comprise means for using the maximum-likelihood-estimated distortion field to generate a matched filter for use in forming a test statistic.
22. The apparatus of claim 20, wherein:
said using means comprise means for taking account of a priori statistics in estimating the distortion field.
23. The apparatus of claim 22, wherein:
said using means comprise means for using a Fourier-space model for taking account of the a priori statistics.
24. The apparatus of claim 15, wherein:
the estimating means comprise means for demodulating the test data preliminary to extracting a distortion field therefrom.

25. The apparatus of claim 22, wherein:
the estimating means comprise means for applying information developed from the reference data as a carrier field, in demodulating the test data.
26. The apparatus of claim 15, wherein the estimating means comprise:
the estimating means comprise means for avoiding errors due to phase shifts greater than half the local periodicity of the assumed carrier field.
27. The apparatus of claim 26, wherein:
the estimating means comprise means for beginning the estimating with a first approximation that is localized and of small magnitude, and iterating so that progressive approximations propagate in the
5 frequency or spatial domain, or both; and
the avoiding means comprise means for controlling rate of propagation to minimize likelihood of introducing a phase shift greater than half the local periodicity in any single iteration.
28. The apparatus of claim 27, wherein the controlling means comprise:
means for monitoring a measure of the rate at which the distortion is changing; and
5 means, responsive to the monitoring means, for limiting the rate of propagation as a function of position, in accordance with said measure.
29. The apparatus of claim 15, wherein the estimating means comprise:
means for providing an assumed carrier field for use in demodulating the test data;
means for analyzing the demodulated test data to approximately
5 ascertain distortion associated with the demodulated test data.
30. The apparatus of claim 15, wherein:
the estimating means comprise means for downsampling the test data according to anticipated degree of abruptness of at least one type of distortion, in preparation for estimating the distortion.

31. The apparatus of claim 30, further comprising:
means for extracting from prior statistics an estimate of the
power spectral density for distortion fields generally; and
means for setting sampling intervals as a function of position,
5 in accordance with the estimate of power spectral density.
32. The apparatus of claim 30:
wherein the estimating means comprise means for downsampling the
test data before estimating the distortion;
further comprising means for applying the estimated distortion to
6 approximately equalize the test and reference data with respect to the
assumed distortion;
further comprising means for interpolating the estimated distortion,
to upsample the estimated distortion for use in the applying
means; and
10 wherein the comparing means compare the thus-approximately-
equalized test and reference data.
33. The apparatus of claim 15, wherein:
the estimating means comprise means for using a gradient search
to estimate the distortion.
34. The apparatus of claim 15, wherein the estimating means comprise:
means for first estimating an isomorphic dilation; and
means for estimating a residual nonisomorphic distortion that
remains after allowing for said estimated isomorphic dilation.

35. Apparatus for verifying the identity of a person by comparing test data representing a two-dimensional test image of that person's skin-pattern print with reference data derived from a two-dimensional reference skin-pattern print image obtained during a prior enrollment
5 procedure, said apparatus comprising:

means for comparing the test data with the reference data to form a test statistic as the ratio, or logarithm of the ratio, of:

likelihood of obtaining the test image, assuming that said
10 person also formed the reference fingerprint image,
and

likelihood of obtaining the test image, assuming that a
different person formed the reference fingerprint
15 image; and

means, responsive to the test statistic, for making an identity-verification decision.

36. The apparatus of claim 35, wherein:

the decision-making means comprise means for comparing the test statistic with a threshold value preselected to impose a desired level of certainty in verification.

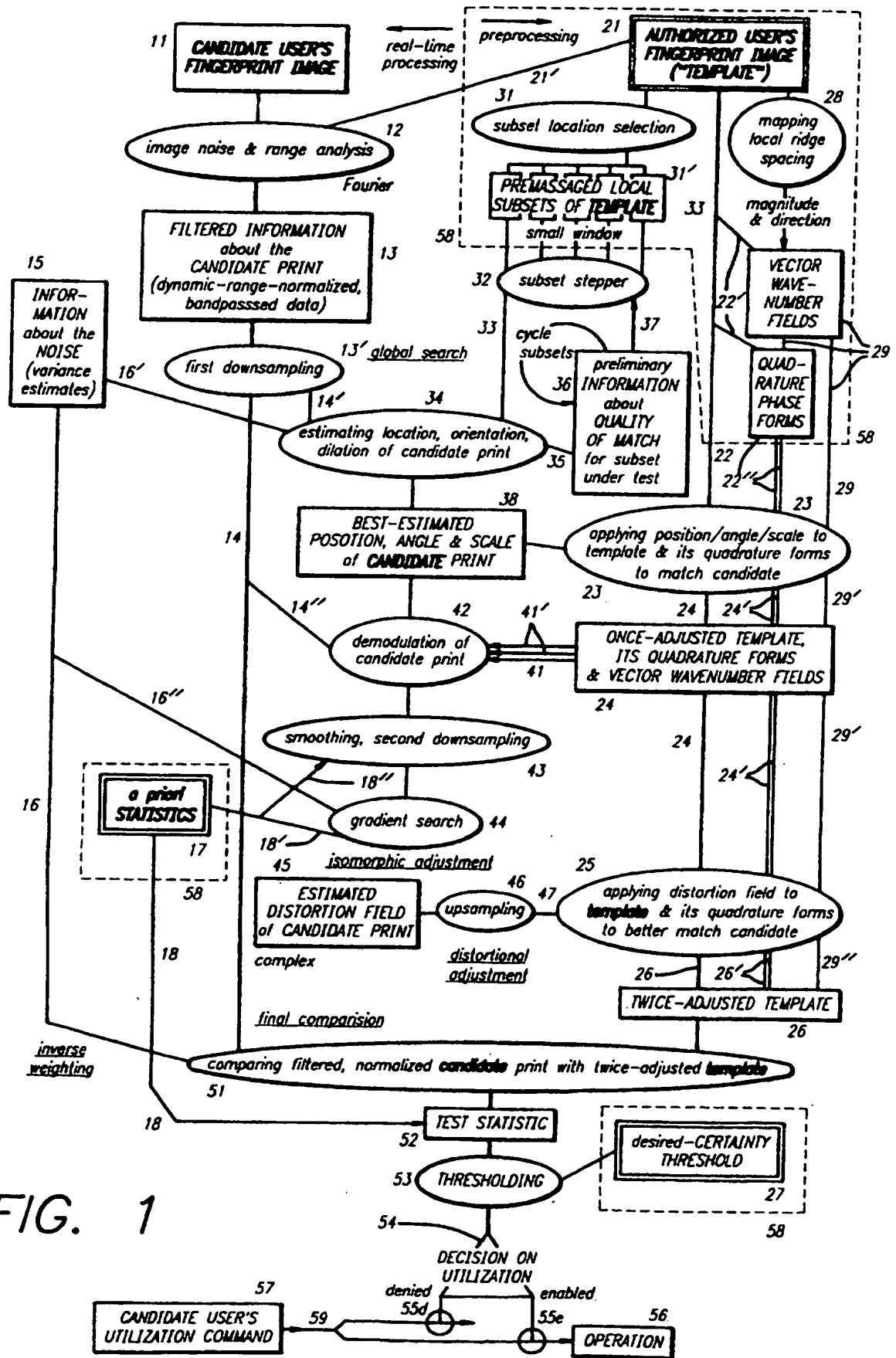
37. A method for verifying the identity of a person by comparing test data representing a two-dimensional test image of that person's skin-pattern print with reference data derived from a two-dimensional reference skin-pattern print image obtained during a prior enrollment
5 procedure, said method comprising the steps of:

extracting from the test data an estimate of noise variance in the test data as a function of position in the test image;

comparing portions of the test and reference data, for corresponding positions in the two images;

10 weighting the importance of comparison for each portion, in accordance with the noise-variance estimate for the corresponding position; and

responsive to the weighting means, making an identity-verification decision.



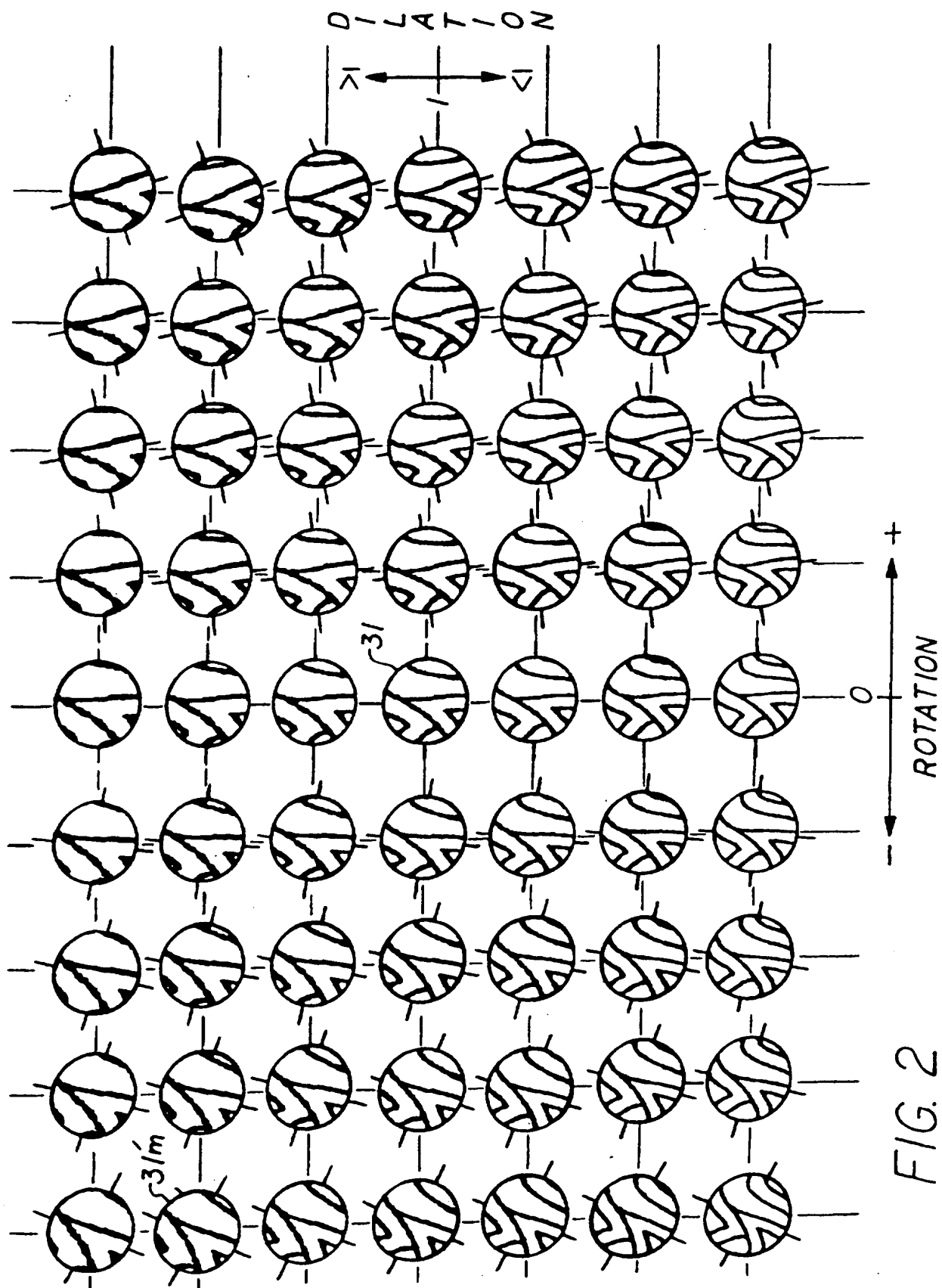


FIG. 2

SUBSTITUTE SHEET (RULE 26)

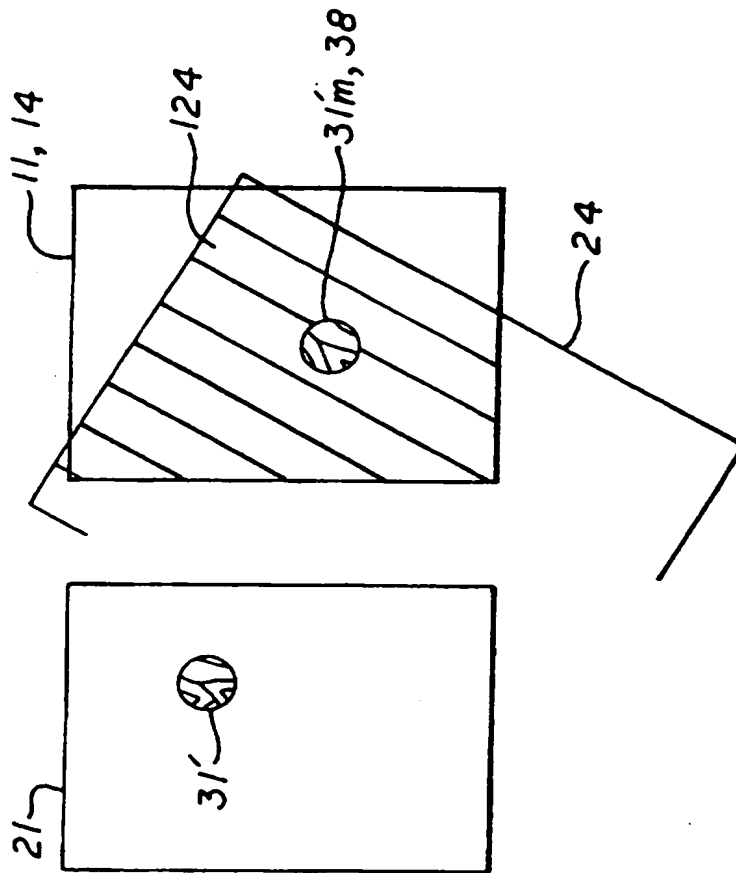
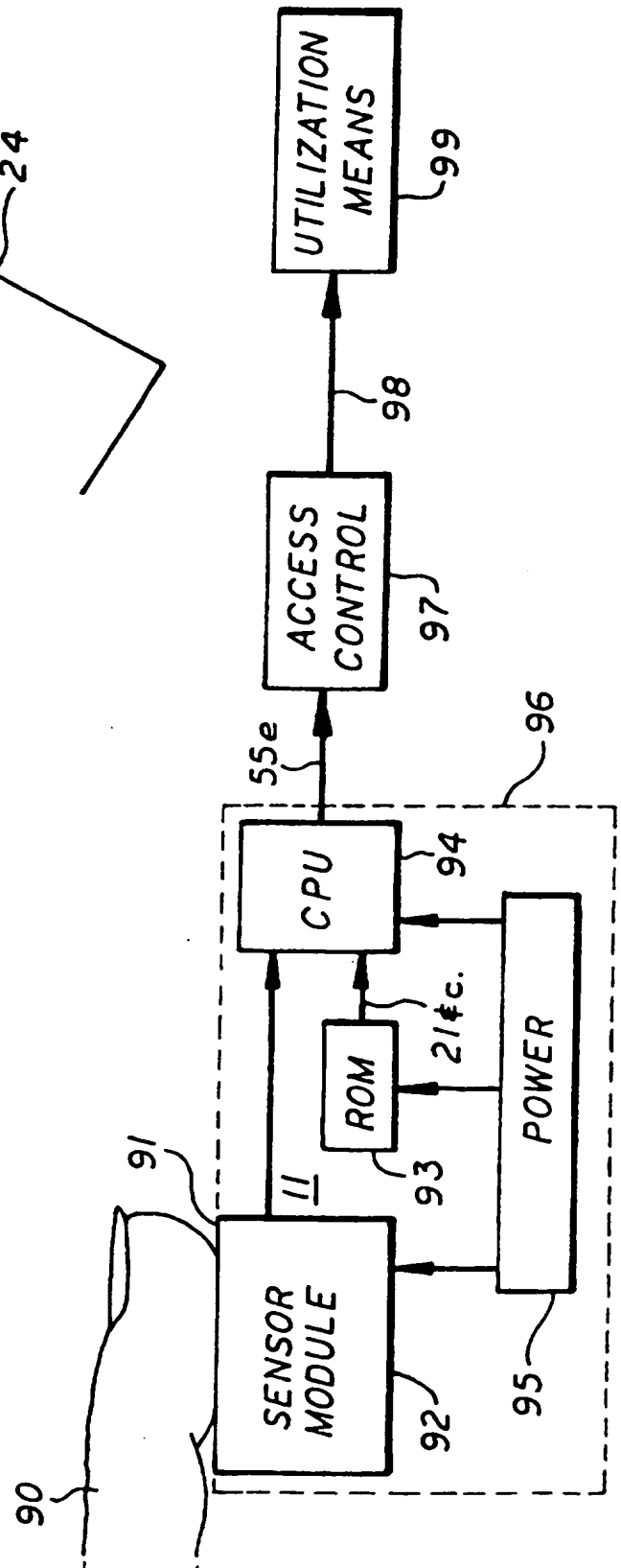


FIG. 8



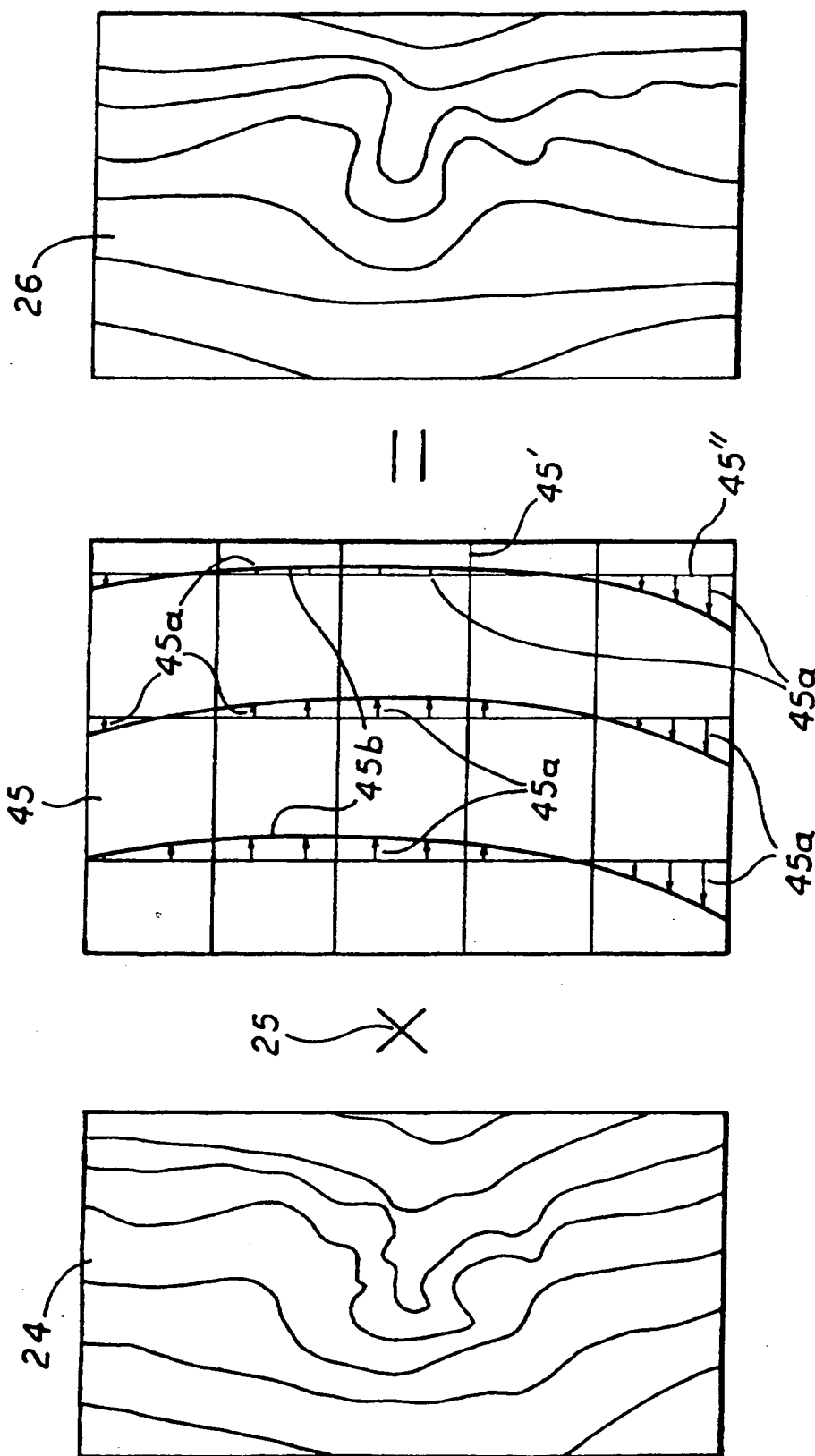
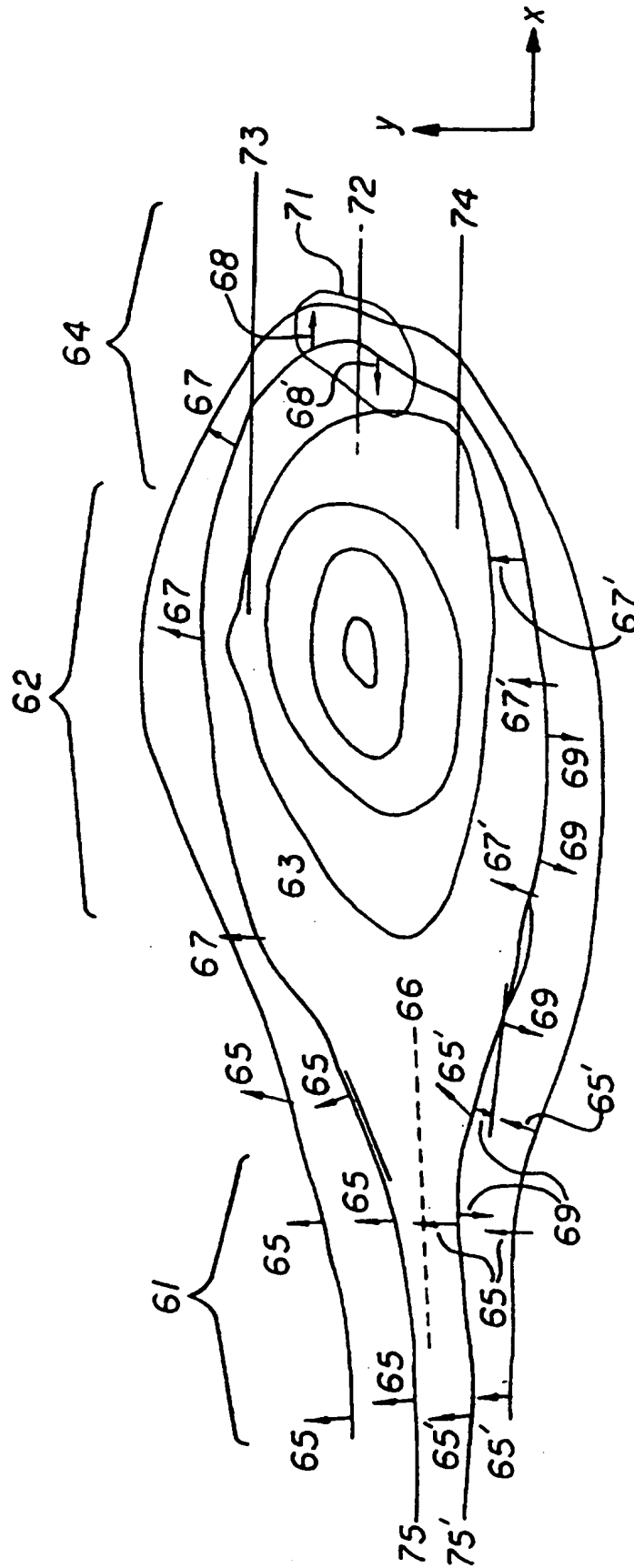


FIG. 4

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FIG. 5



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FIG. 6

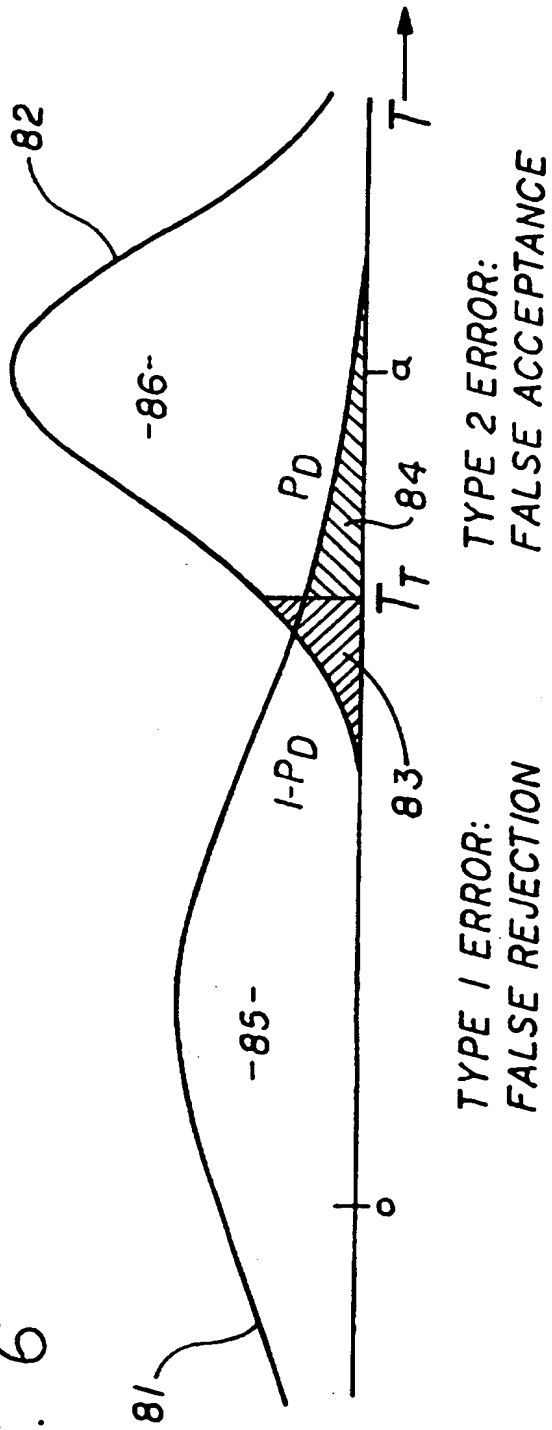
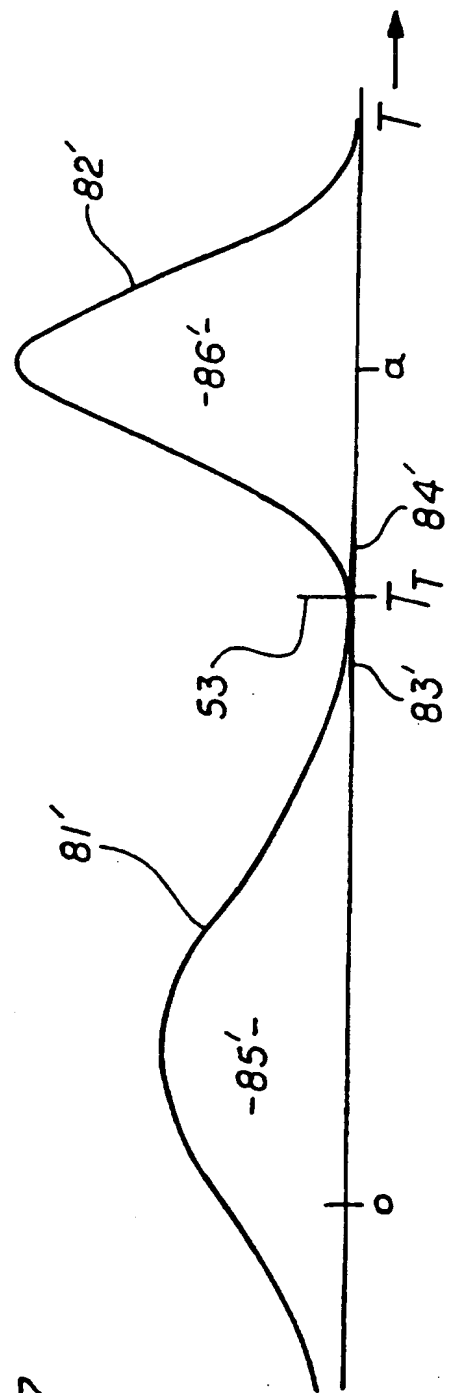


FIG. 7



INTERNATIONAL SEARCH REPORT

International application No.
PCT/US97/16580

A. CLASSIFICATION OF SUBJECT MATTER

IPC(6) : G06K 9/00, 9/36, 9/40

US CL : 382/124, 125, 209, 254, 275, 278, 280

According to International Patent Classification (IPC) or to both national classification and IPC

B. FIELDS SEARCHED

Minimum documentation searched (classification system followed by classification symbols)

U.S. : 382/124, 125, 209, 254, 275, 278, 280, 115, 116, 126, 127, 206, 207, 218, 256, 257, 260, 274, 279, 280

Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched

Electronic data base consulted during the international search (name of data base and, where practicable, search terms used)

APS, MAYA, IEEE DATABASE

search terms: fingerprint, noise, ridge spacing and direction, dilation, distortion, test statistic

C. DOCUMENTS CONSIDERED TO BE RELEVANT

Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
Y	US 4,811,414 A (FISHBINE et al) 07 March 1989, abstract, col. 3, lines 13-55, col. 16, line 46 - col. 19, line 54.	1, 12, 37
Y	US 5,040,223 A (KAMIYA et al) 13 August 1991, abstract, figures 5 and 8, col. 6, lines 59 - 68.	1, 12, 37
Y	US 5,351,304 A (YAMAMOTO) 27 September 1994, abstract, figure 1 : 1-2, 1-3 & 1-4.	2-4, 12
Y	US 3,959,884 A (JORDAN et al) 01 June 1976, abstract, figures 17 & 20.	2-4, 12
Y	US 5,067,162 A (DRISCOLL, Jr. et al) 19 November 1991, abstract, col. 4, lines 16-26.	2-4, 12

☒ Further documents are listed in the continuation of Box C. ☐ See patent family annex.

* Special categories of cited documents:	*T	later document published after the international filing date or priority date and not in conflict with the application but cited to understand the principle or theory underlying the invention
A document defining the general state of the art which is not considered to be of particular relevance	*X*	document of particular relevance; the claimed invention cannot be considered novel or cannot be considered to involve an inventive step when the document is taken alone
B earlier document published on or after the international filing date	*Y*	document of particular relevance; the claimed invention cannot be considered to involve an inventive step when the document is combined with one or more other such documents, such combination being obvious to a person skilled in the art
L document which may throw doubts on priority claim(s) or which is cited to establish the publication date of another citation or other special reason (as specified)	*A*	document member of the same patent family
O document referring to an oral disclosure, use, exhibition or other means		
P document published prior to the international filing date but later than the priority date claimed		

Date of the actual completion of the international search

19 JANUARY 1998

Date of mailing of the international search report

11 FEB 1998

Name and mailing address of the ISA/US

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INTERNATIONAL SEARCH REPORT

International application No.

PCT/US97/16580

C (Continuation). DOCUMENTS CONSIDERED TO BE RELEVANT

Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
Y	US 4,983,036 A (FROELICH) 08 January 1991, abstract, figure 4, col. 6, lines 23-33.	5-6, 12
Y	US 5,530,772 A (STOREY) 25 June 1996, abstract, figures 1-2, col. 2, lines 33-47.	5-6, 12
Y, P	US 5,619,596 A (IWAKI et al) 08 April 1997, abstract, Figures 1-2.	4-6, 12
Y	US 4,208,651 A (MCMAHON) 17 June 1980, abstract, col. 5, lines 54 - col. 7, lines 50, especially col 6, lines 27-31.	6-7, 12
X, P	US 5,659,626 A (ORT et al) 19 August 1997, abstract, figures 6-9.	7, 12
X, P	US 5,555,314 A (NAKAJIMA) 10 September 1996, abstract, figures 1-2.	8-14
X	US 4,641,350 A (BUNN) 03 February 1987, abstract, col. 6, lines 34-67, col. 8, lines 3-46.	15-16
A		17-34
A	US 5,105,467 A (KIM et al) 14 April 1992, abstract.	35-36
A	US 4,956,870 A (HARA) 11 September 1990, abstract, figures 1-3.	35-36

INTERNATIONAL SEARCH REPORT

International application No.
PCT/US97/16580

Box I Observations where certain claims were found unsearchable (Continuation of Item 1 of first sheet)

This international report has not been established in respect of certain claims under Article 17(2)(a) for the following reasons:

1. ☐ Claims Nos.:
because they relate to subject matter not required to be searched by this Authority, namely:

2. ☐ Claims Nos.:
because they relate to parts of the international application that do not comply with the prescribed requirements to such an extent that no meaningful international search can be carried out, specifically:

3. ☐ Claims Nos.:
because they are dependent claims and are not drafted in accordance with the second and third sentences of Rule 6.4(a).

Box II Observations where unity of invention is lacking (Continuation of Item 2 of first sheet)

This International Searching Authority found multiple inventions in this international application, as follows:

Please See Extra Sheet.

1. ☒ As all required additional search fees were timely paid by the applicant, this international search report covers all searchable claims.
2. ☐ As all searchable claims could be searched without effort justifying an additional fee, this Authority did not invite payment of any additional fee.
3. ☐ As only some of the required additional search fees were timely paid by the applicant, this international search report covers only those claims for which fees were paid, specifically claims Nos.:

4. ☐ No required additional search fees were timely paid by the applicant. Consequently, this international search report is restricted to the invention first mentioned in the claims; it is covered by claims Nos.:

Remark on Protest

- ☐ The additional search fees were accompanied by the applicant's protest.
- ☒ No protest accompanied the payment of additional search fees.

BOX II. OBSERVATIONS WHERE UNITY OF INVENTION WAS LACKING

This ISA found multiple inventions as follows:

This application contains the following inventions or groups of inventions which are not so linked as to form a single inventive concept under PCT Rule 13.1. In order for all inventions to be searched, the appropriate additional search fees must be paid.

Group I, claim(s) 1, 37 and 12, drawn to an apparatus and method for verifying an identity of a person by extracting an estimate of noise variance in the test data.

Group II, claim(s) 2-4 and 12, drawn to an apparatus for verifying an identity of a person by deriving multilevel test data that are bandpassed and normalized.

Group III, claim(s) 5-6 and 12, drawn to apparatus for verifying an identity of a person by expressing test data and reference data in the form of local sinusoids.

Group IV, claim(s) 7 and 12, drawn to apparatus for verifying an identity of a person by deriving from the reference data a map of ridge spacing and direction.

Group V, claim(s) 8-14, drawn to apparatus for verifying an identity of a person by estimating the assumed dilation of the test image relative to a reference image.

Group VI, claim(s) 15-34, drawn to apparatus for verifying an identity of a person by estimating an assumed distortion of the test image.

Group VII, claim(s) 35-36, drawn to apparatus for verifying an identity of a person by comparing a test data with reference data to form a test statistics as the ratio.

The inventions listed as Groups I-VII do not relate to a single inventive concept under PCT Rule 13.1 because, under PCT Rule 13.2, they lack the same or corresponding special technical features for the following reasons: the special technical feature of the Group I invention is means for extracting an estimate of noise variance in the test data as a function of position in the test image; the special technical feature of the Group II invention is means for deriving multilevel test data that are bandpassed and normalized; the special technical feature of the Group III invention is the means for expressing the test data and the reference data in the form of local sinusoids; the special technical feature of the Group IV invention is the means for deriving from the reference data a map of ridge spacing and direction; the special technical feature of the Group V invention is the means for estimating the assumed dilation of the test image relative to a reference image; the special technical feature of the Group VI invention is the means for estimating an assumed distortion of the test image; and the special technical feature of the Group VII invention is the means for comparing test data with the reference data to form a test statistic as the ratio. Since the special technical feature of any one Group is not present in any of the other Groups, unity of invention is lacking.